

# TYA - HOU-SalsaJ

## L'Allée des étoiles, Alley of the stars

tutorial with Hands-On-Universe group ([www.eu-hou.net](http://www.eu-hou.net))

*Lying on the vacoas cloth, wrapped with Ouma up in (a military) blanket, I look up at the stars..., I speak out their names, as I used to do with my dad, walking down (our garden Alley, that we called ) Alley of the stars: Arcturus, Denebola, Bellatrix, Bételgeuse, Acomar, Antarès, Shaula, Altaïr, Andromède, Fomalhaut.*

J-M.G. Le Clézio, 1985, in *The gold digger* . Literature Nobel Prize 2008.

Suzanne Faye, Lycée Chaptal, Paris  
Michel Faye, Lycée Louis-le-Grand, Paris  
[mfaye2@wanadoo.fr](mailto:mfaye2@wanadoo.fr)

# SalsaJ european free software on [www.eu-hou.net](http://www.eu-hou.net)

The screenshot shows the EU-HOU website's download section for SalsaJ. The top navigation bar includes links for Home, What is EU-HOU?, The software (with sub-links for Download, Manual, F.A.Q.), Exercises, Tools, Forums, News, and Important dates. A search bar is also present. The main content area features a green header with a stick figure icon and the word "Download". Below this, there is a sub-header "The new version 1.1 of SalsaJ" with a small icon of a hand holding a disc. The main text describes SalsaJ as a Java-based software for astronomical image handling and analysis, developed by Wayne Rasband. It mentions that it is based on ImageJ, a free Java software. At the bottom, there is a logo for "For PC Windows :" and a note about Java installation and file download.

**HOU =**

**Hands-On-Universe**  
[www.handsonuniverse.org](http://www.handsonuniverse.org)

**F-HOU,**

**France Hands-On-Universe**  
[www.eu-hou.net](http://www.eu-hou.net)

**EU-HOU,**

**Europe Hands-On-Universe**  
[www.eu-hou.net](http://www.eu-hou.net)

# Happy Hands-On-Universe

Follow Balthus, Miro,  
the little Prince.  
Meet cats  
and  
dance with a galaxy.

F-HOU  
Fun-HOU  
France-HOU  
Friends-of-HOU





# Happy Hands-On-Universe

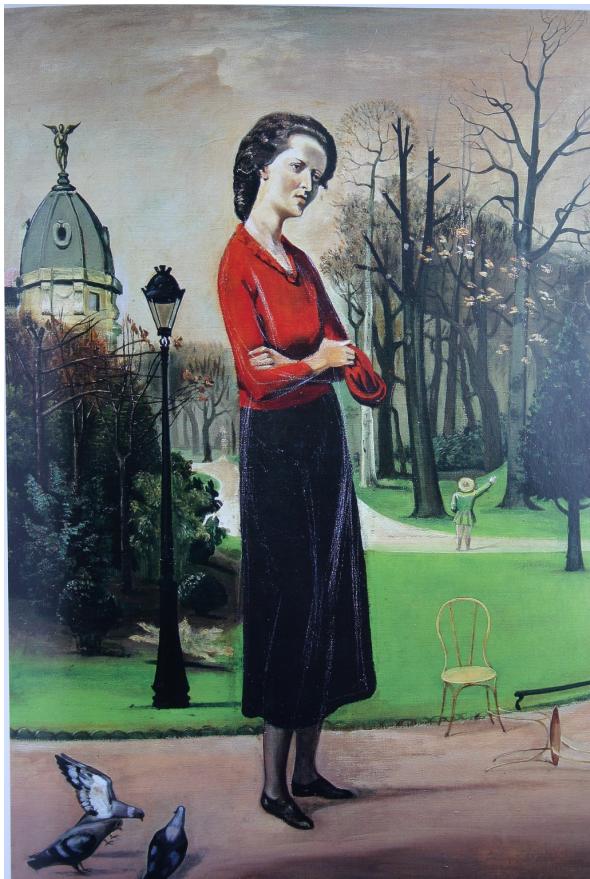
What you find on the CD:

Binary system Dossier de fichiers	Cepheids Dossier de fichiers	Dancing with a galaxy Dossier de fichiers	Supernovae Dossier de fichiers
TRACKING_JUPITERS_MOONS Dossier de fichiers	RedMoonCat Fichier 1 629 Ko	BalthusCat Image JPEG 3072 x 2048	HookedGalaxyESO Image JPEG 400 x 632
MiroMoonMosaic Image JPEG 1194 x 922	Moon Image JPEG 761 x 787	RedMoonCat Image JPEG 751 x 1106	Sun Image JPEG 640 x 480
Unesco2009 Présentation Microsoft Power... 16 512 Ko	UnescoBooklet Présentation Microsoft Power... 7 823 Ko	SalsaJ_V1.1-Windows Dossier de fichiers	

All the texts are in English, except  
the french text inside cepheids file

Open (or set up) SalsaJ, then Balthus'Cat

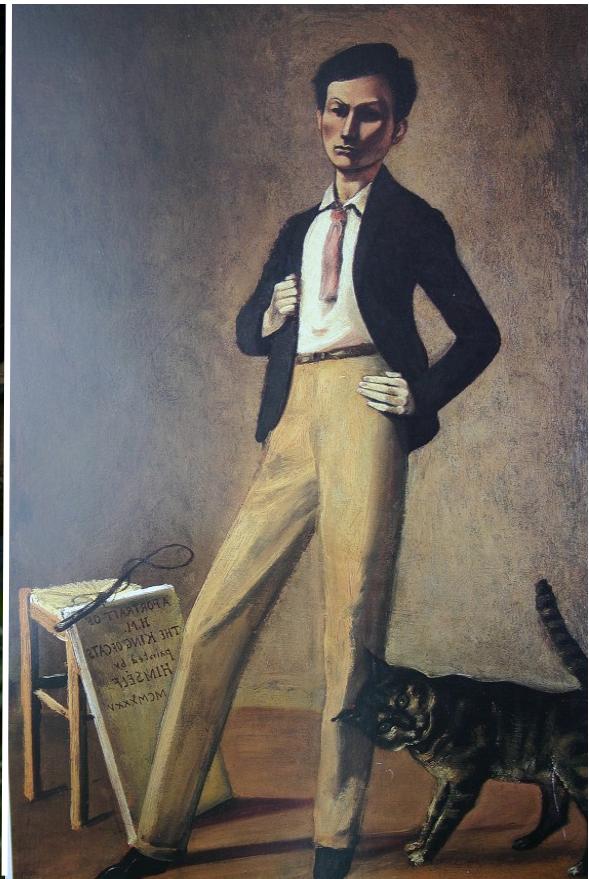
First step : Paris, Balthus, cats and SalsaJ (free software on [www.eu-hou.net](http://www.eu-hou.net))



In the garden of  
Champs-Elysées  
*painted by Balthus*



Odeon Theater and  
french restaurant  
Mediterranean Sea

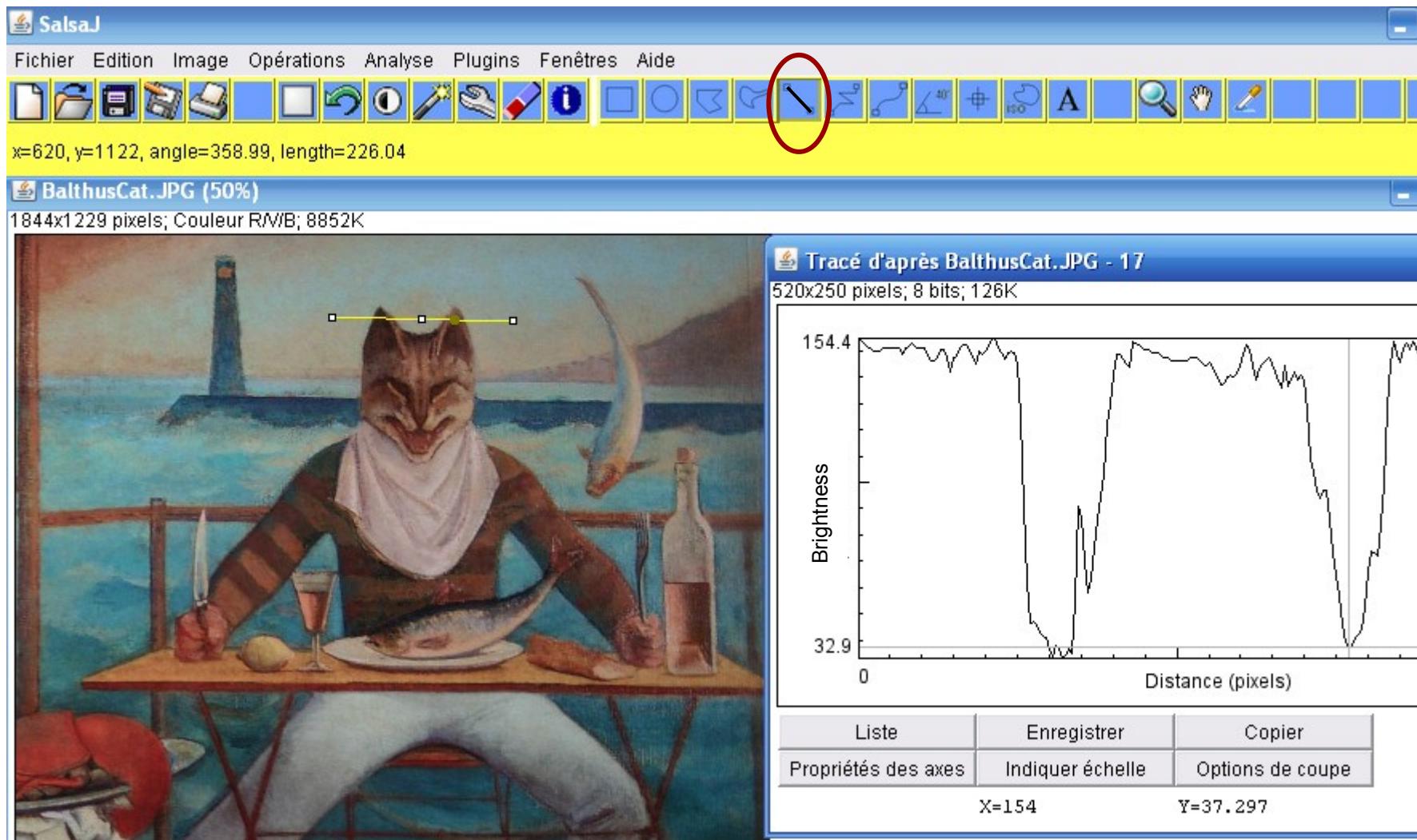


Balthus, french painter,  
the King of cats  
*self-portrait*

File/Open image /Balthus'Cat  
(sign of Odeon restaurant)

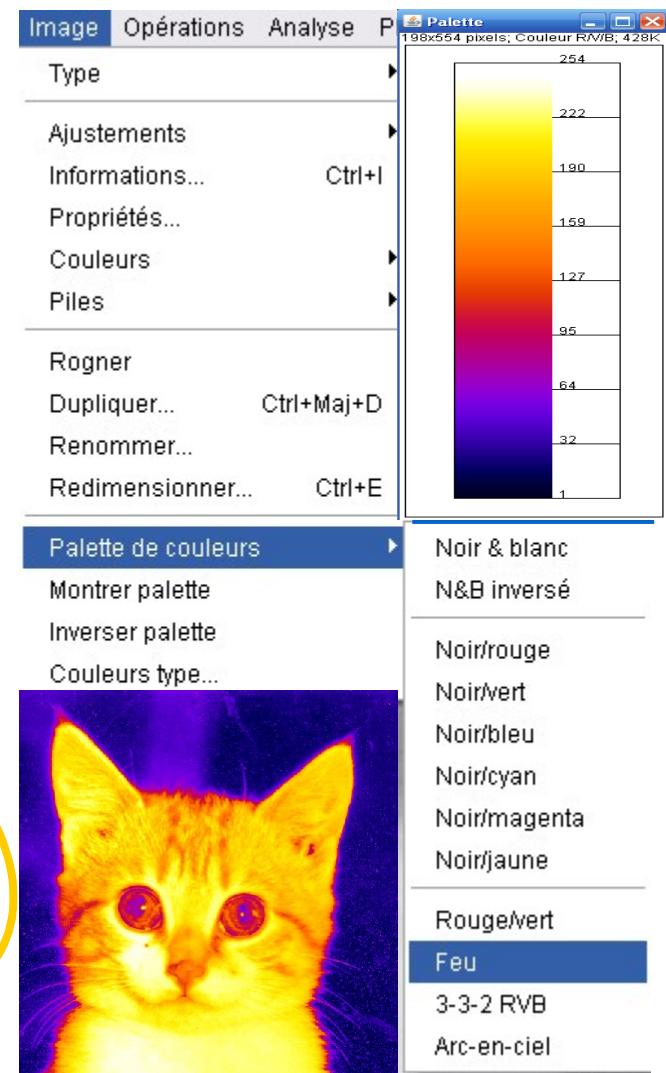
Draw a line through the ears of the cat

Go to Analyse/ Plot Profile





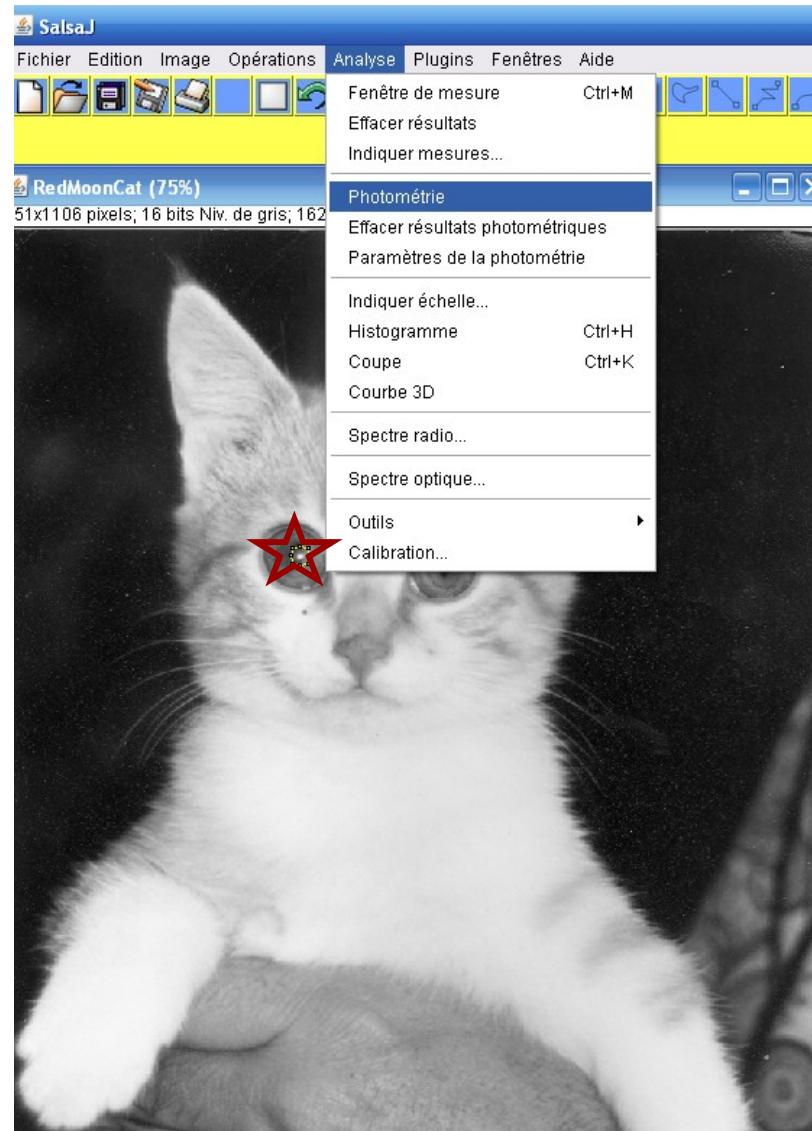
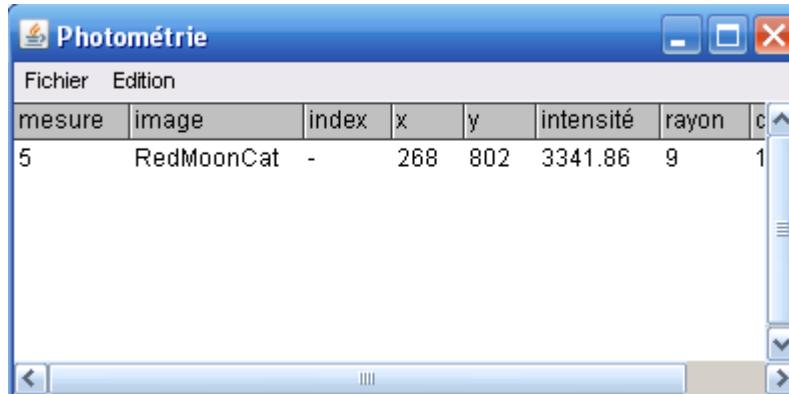
# Play with the image of Red Moon Cat



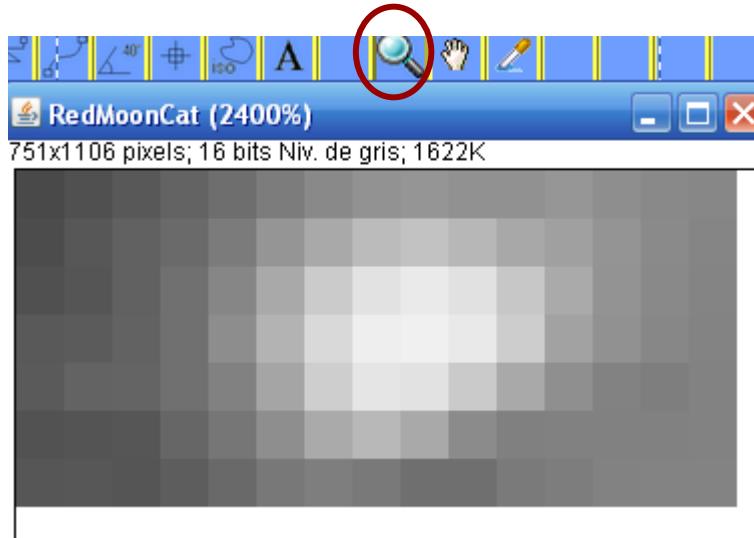
File/Open image  
/RedMoonCat.fts

Photometry needs a grey  
levels image.fts

Go to Analyse/Photometry



Use SalsaJ magnifying glass to see pixels:



Second step: Paris, Unesco;  
see Miro's sun and moon mosaics

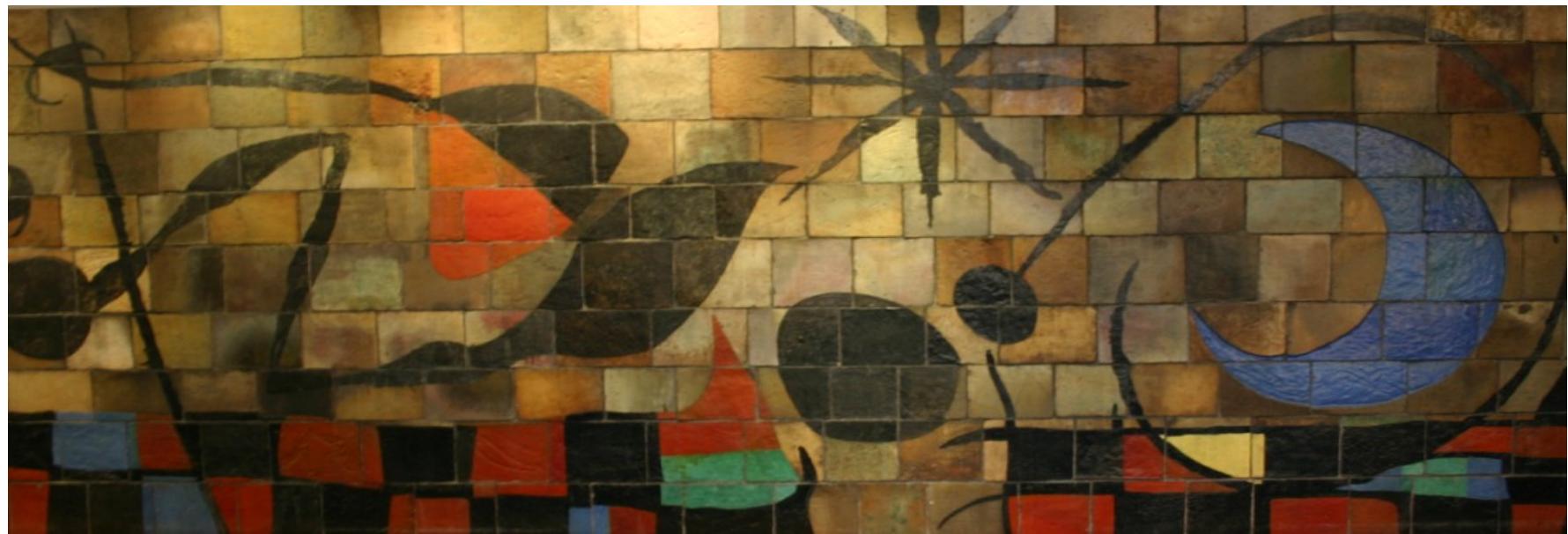


Screenshot of a software interface showing the 'Image' menu open. The 'Image' option is highlighted with a red oval. The 'Informations...' option is also highlighted with a red oval. The right panel displays image information for 'Miro.JPG'.

- Image** Opérations Analyse Plugins Fenêtres Aide
- Type
- Ajustements
- Informations... Ctrl+I**
- Propriétés...
- Couleurs
- Piles
- Roger
- Duplicer... Ctrl+Maj+D
- Renommer...
- Redimensionner... Ctrl+E
- Palette de couleurs
- Montrer palette
- Inverser palette
- Couleurs type...

Info for Miro.JPG  
Fichier Edition

Title: Miro.JPG  
Width: 1194 pixels  
Height: 922 pixels  
Bits per pixel: 32 (RGB)  
No Threshold  
Magnification: 0.75  
*In astronomy images,  
the image information will give  
date, observatory, wavelength ...*



## To compare stars and planets – SalsaJ Plot Profile

Our  
moon

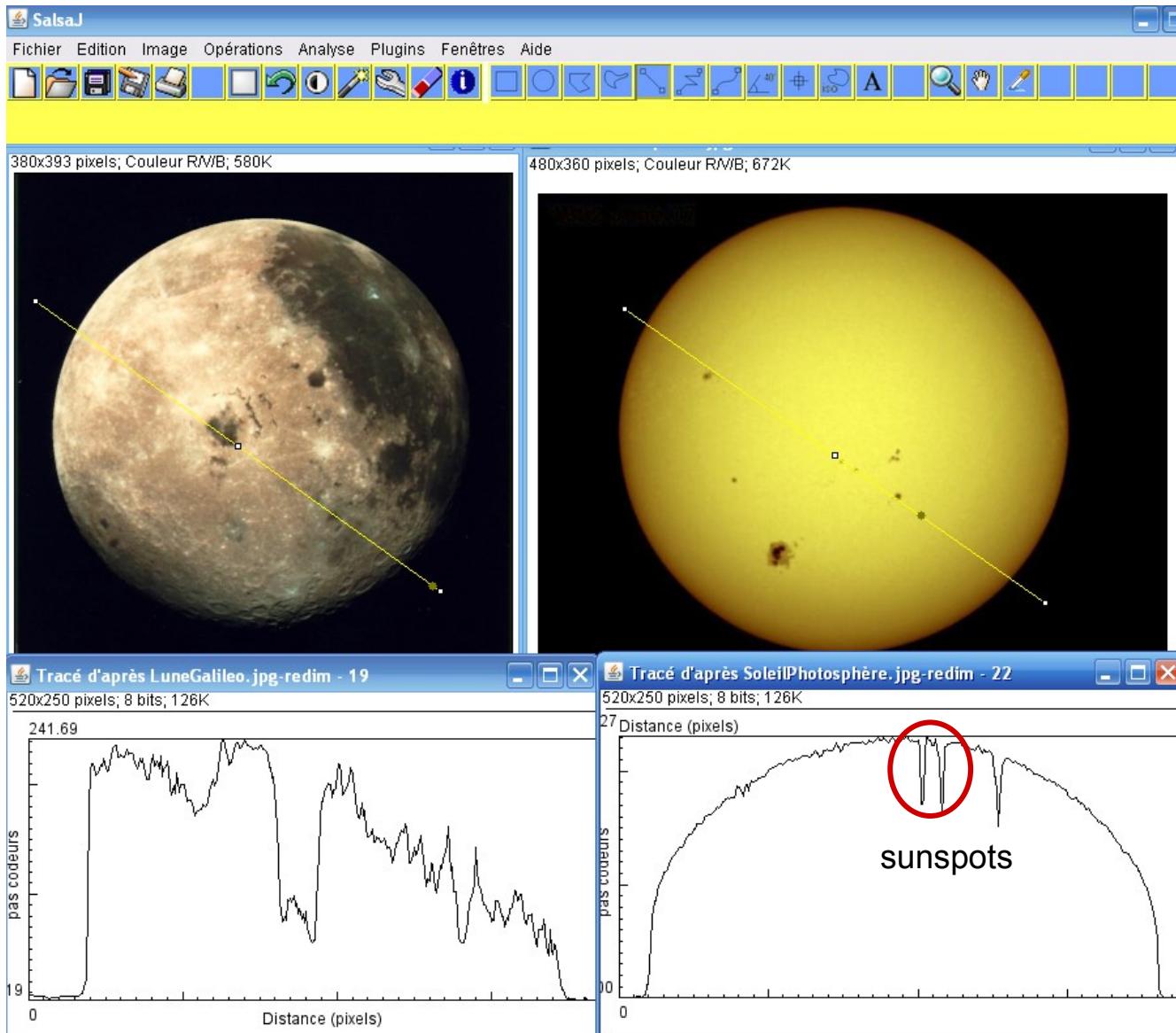
No  
atmosphere

Mounts  
and valleys

Our Sun:

Gaz(plasma)  
atmosphere

Sunspots

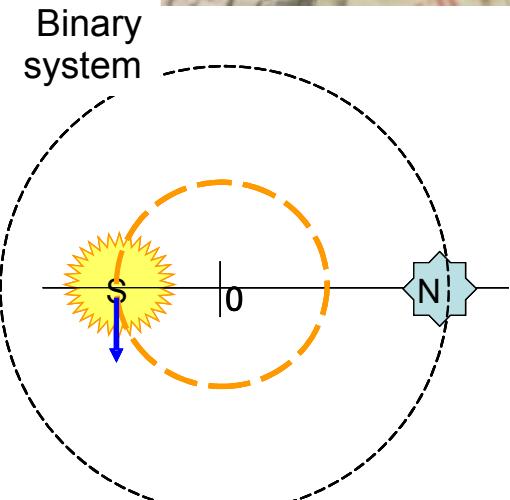


### 3rd step: In 2009, the Little Prince comes from an exoplanet

1943, Saint-Exupéry, french writer and aviator wrote:



*I have serious reason to believe that the planet  
from which the little prince came is the asteroid  
B 612.*

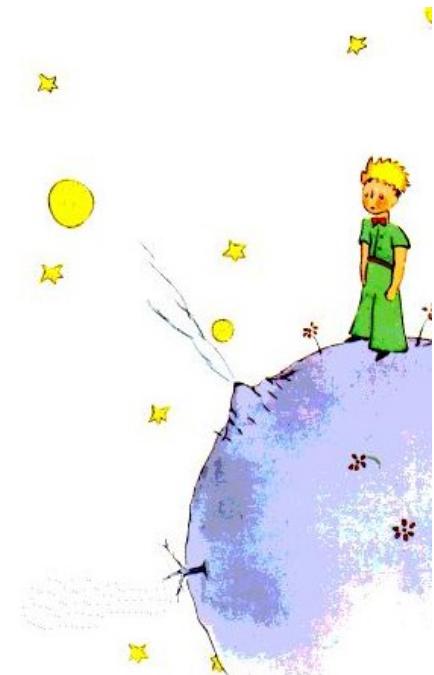


S= Star

N = Non identified companion

O= barycentre

2009 : Does the little  
prince lives on an  
exoplanet?



## Seven steps for a dwarf star : from Doppler to exoplanets



Education and Culture

**Socrates**  
Minerva



### Seven steps for a dwarf star

From Doppler to exoplanets ▾

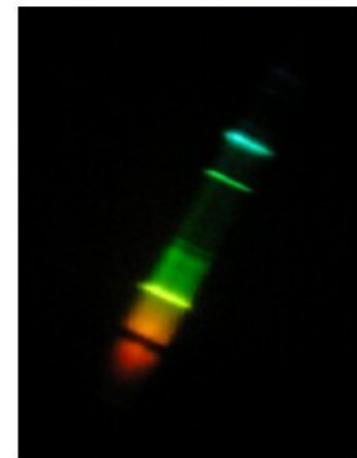
- Exercice proposed by :  
**Roger FERLET**, Institut d'Astrophysique de Paris, France  
**Michel FAYE**, lycée Louis Le Grand , Paris , France  
**Suzanne FAYE**, Lycée Chaptal , Paris , France



Summary :

- SPECTROSCOPY
- ANIMATED MOTION OF SPECTRUM LINES
- MEASURE WAVELENGTH  $\lambda$  AND FLUX, OPTICAL SPECTRUM
- CALCULATING RADIAL VELOCITY OF THE STAR WITH DOPPLER SHIFT
- RADIAL VELOCITY OF THE STAR , AS A FUNCTION OF DATE
- DETERMINING THE MASS OF THE COMPANION IN BINARY SYSTEM
- DISCOVERING AN EXOPLANET WITH DOPPLER SHIFT OF A STAR

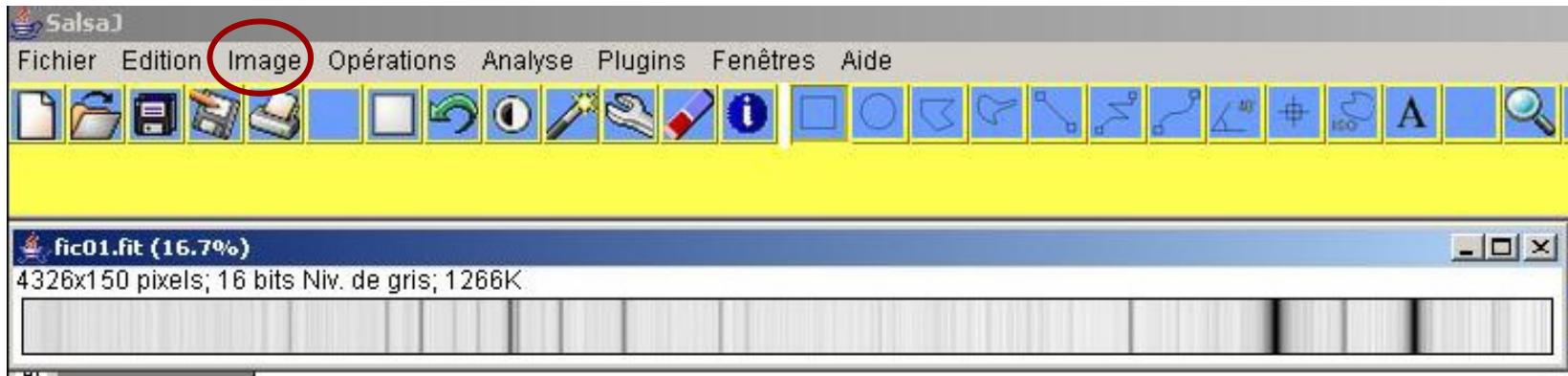
Download the exercise : [pdf 317.75 Kb](#)



## ANIMATED MOTION OF SPECTRUM LINES

### USE images.fit

Note : images.fit (fit =fits = fts) are available for animation  
images.dat are available for optical spectra

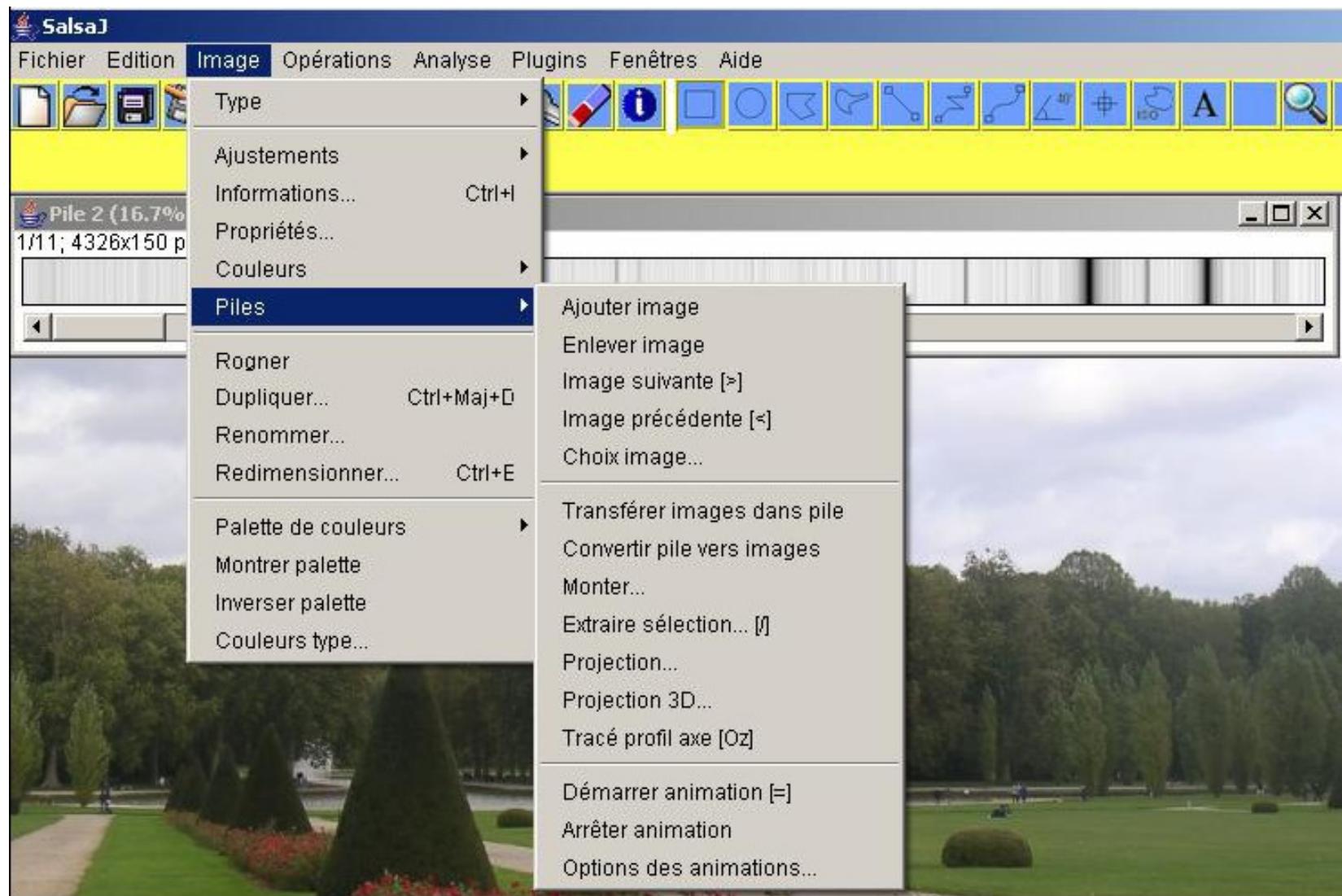


To have a global view of Doppler shift when the star moves around barycenter:  
With Salsa J, **Open (Ouvrir)** folder (dossier) : ***binary system***

Select the 11 spectra images.fit from fic01.fit to fic11.fit : press Shift to select the 11images.fit at once.

**Open (Ouvrir)** these 11 images, then click on **Images** : you get a roll-down menu ; click on **Stacks (=Pile)** : you get a new menu ; click on **Transfer Images to Stacks (=Transférer images dans Pile)**

Click again on **Images / Stacks (=Piles)** ; then **Images/Start animation (=Démarrer animation)**

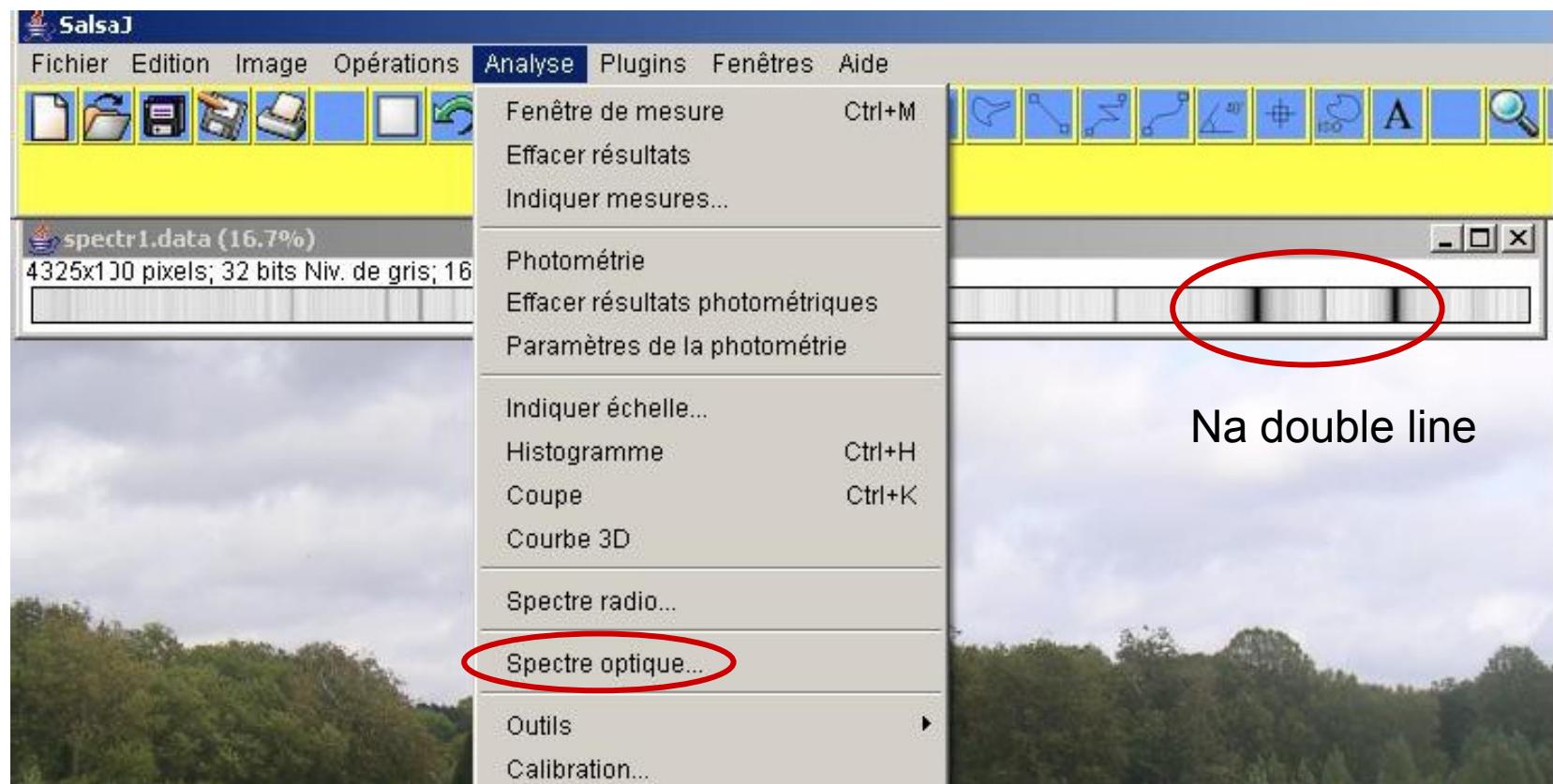


# MEASURE WAVELENGTH $\lambda$ AND FLUX, OPTICAL SPECTRUM

## Use images.dat

### Investigation of spectrum 1 : spectr 1.data

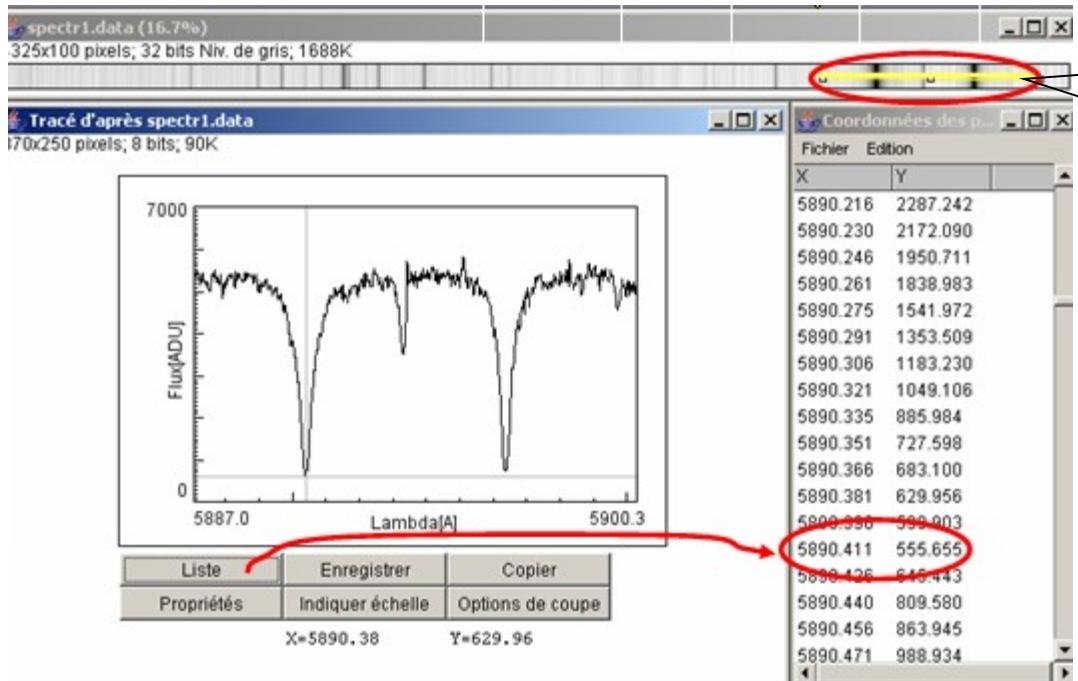
Click on Analysis / Optical Spectrum/ binary system / spectr1.data



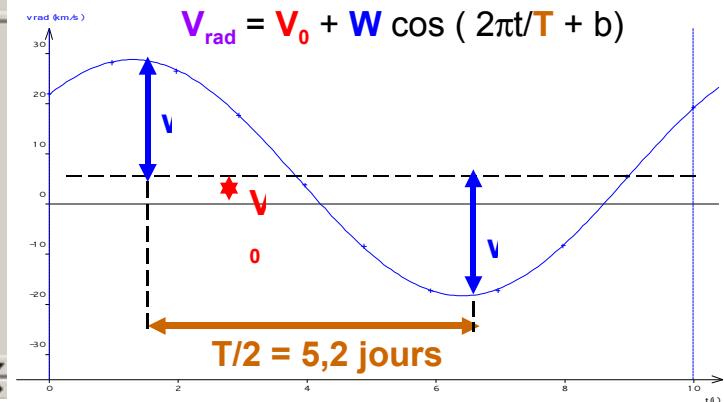
## Flux according to wavelength : $\Phi = f(\lambda)$

Spect1.dat image / Click on the **Straight line selection (Sélection rectiligne)** icon, then draw a straight line **across the Na doublet** (to have an horizontal line, press Shift during the drawing)

Click on **Analysis / Plot Profile (=Coupe)** : you get  $\Phi = f(\lambda)$

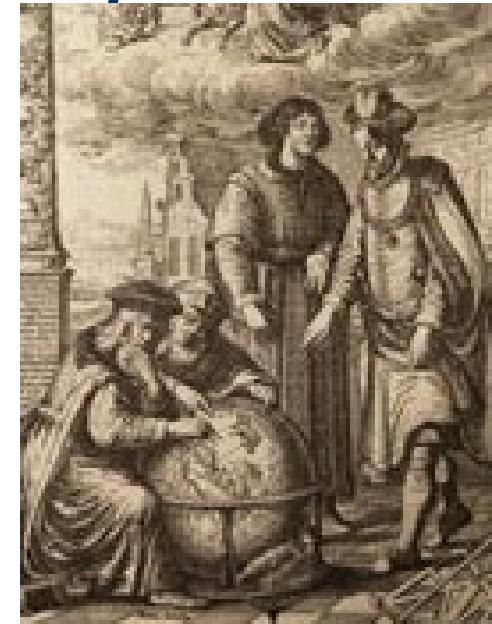


*On suit les raies du doublet jaune du sodium pendant plusieurs jours*



**4th step** : SalsaJ with Galileo spectacles

## *Christmas 1604 : the new star was a supernova*



1604 :

A young teacher discovers a new star in the sky (Galileo, october 1604)

Shakespeare begins to write « Hamlet », inspired by Tycho Brahe (the man with a golden nose)

**1608: Lippershey, a spectacles vendor, introduces the first « optical pipe» as spyglasses**

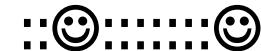
1582 : *The Spectacle Vendor* by Johannes Stradanus, engraved by Johannes Collaert



**1609: Galileo is the first one to use it as a refractor telescope**



**1610: Galileo publishes « The Sidereal Messenger »**



1610:

Galilean  
Moons

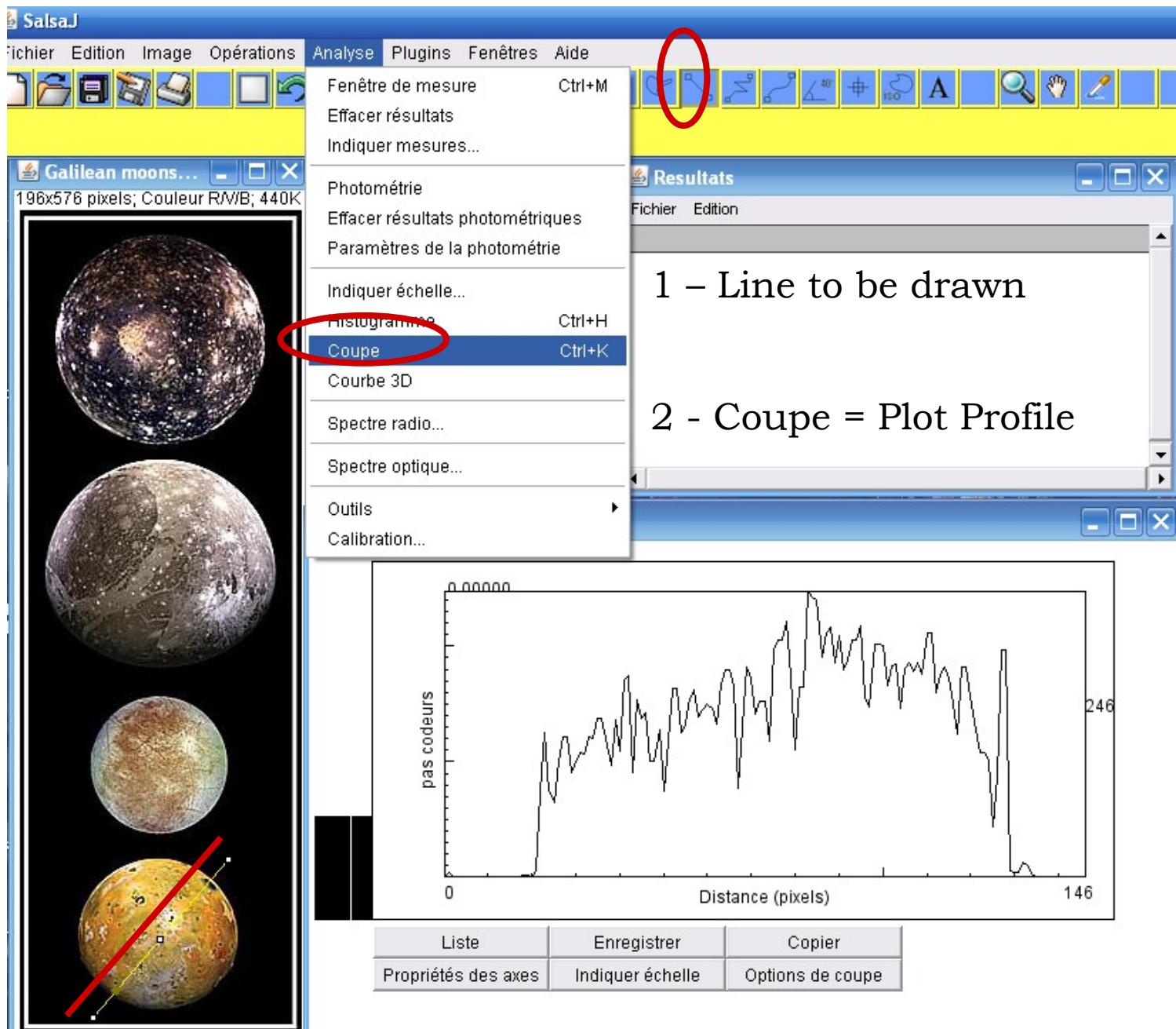
Callisto

Ganymède

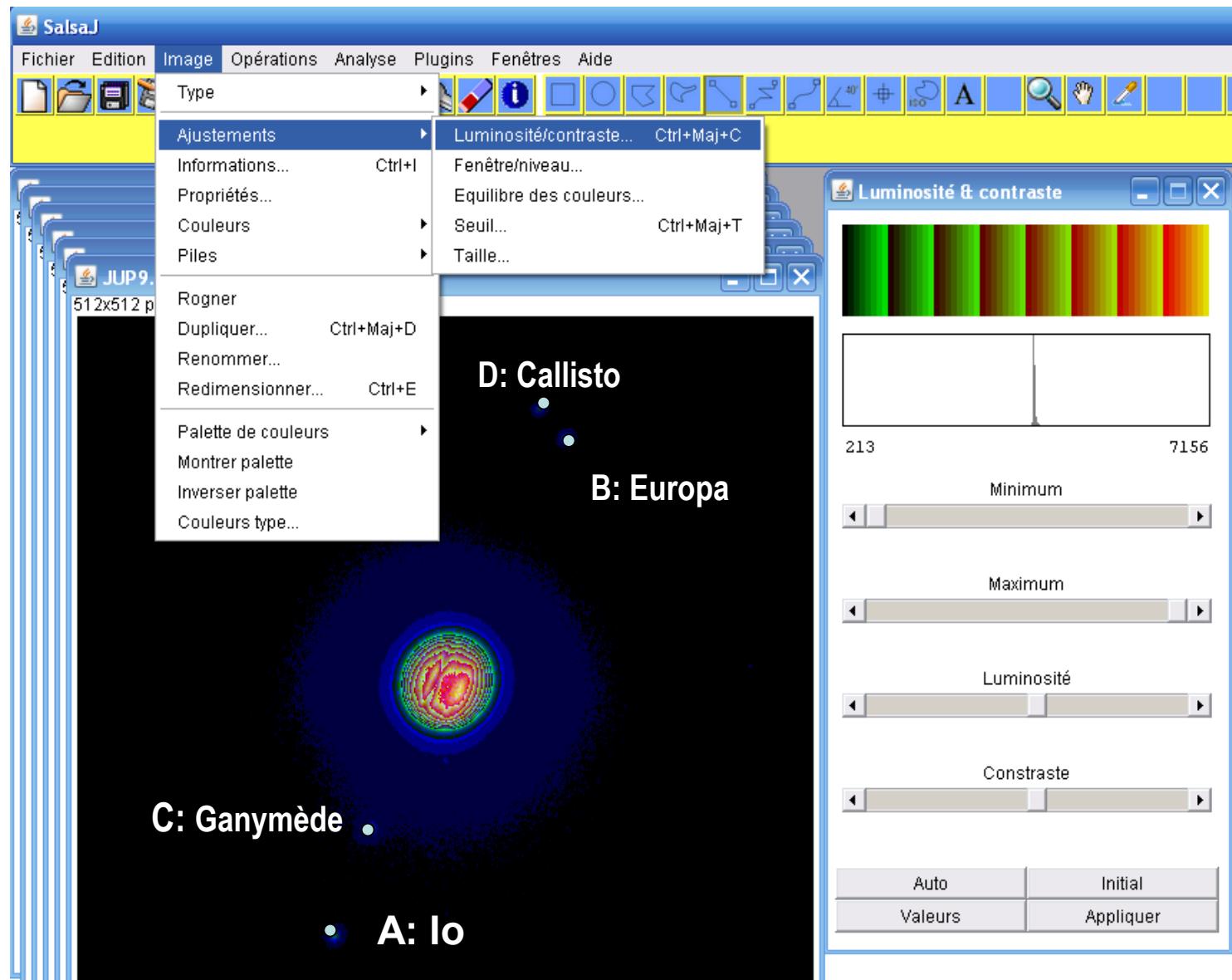
Europe

Io

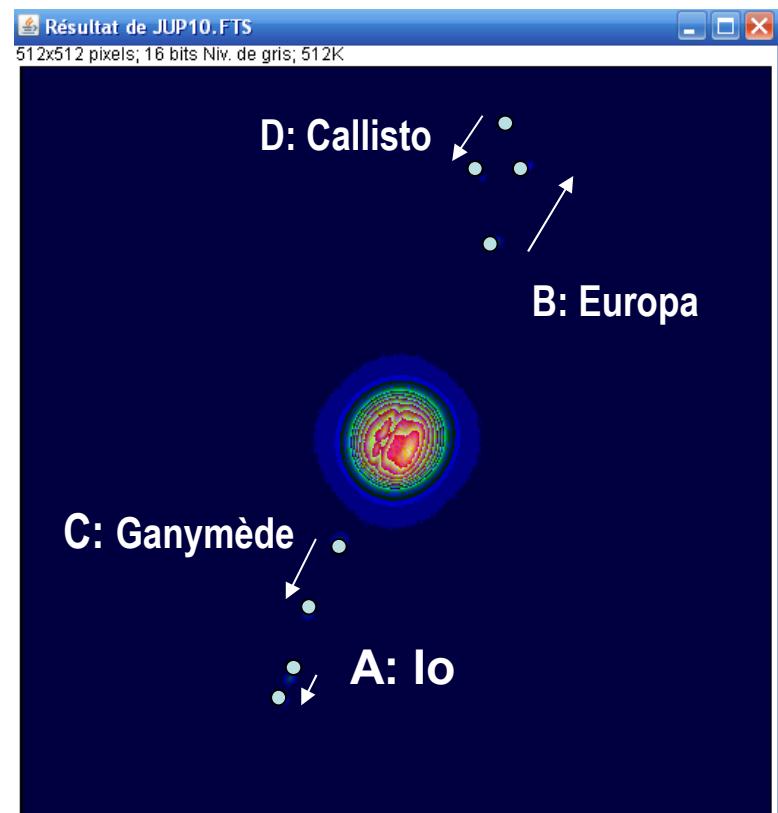
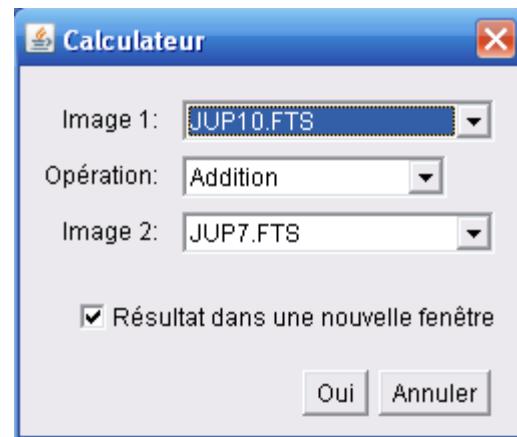
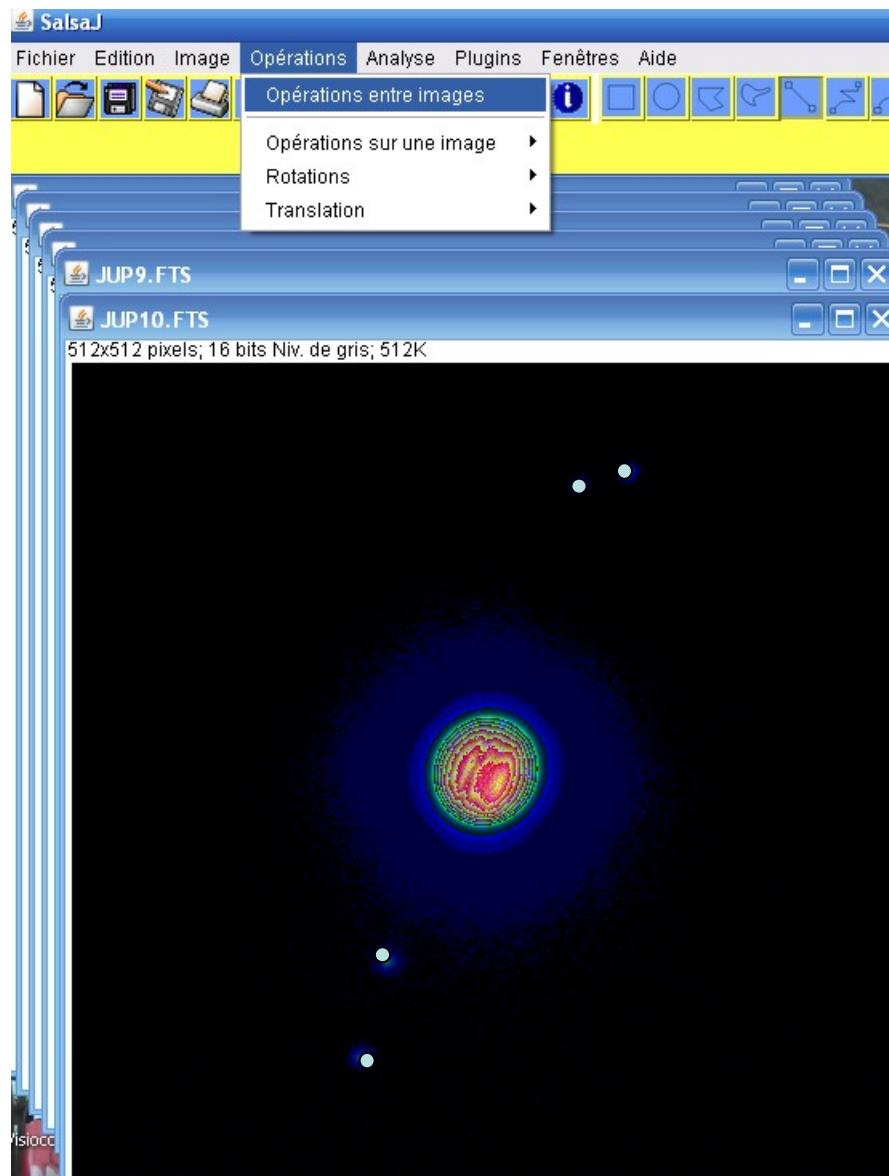
Credit NASA



### III – SalsaJ Operations: Jupiter's Galilean Moons



# Add images (or subtract ...)





SalsaJ



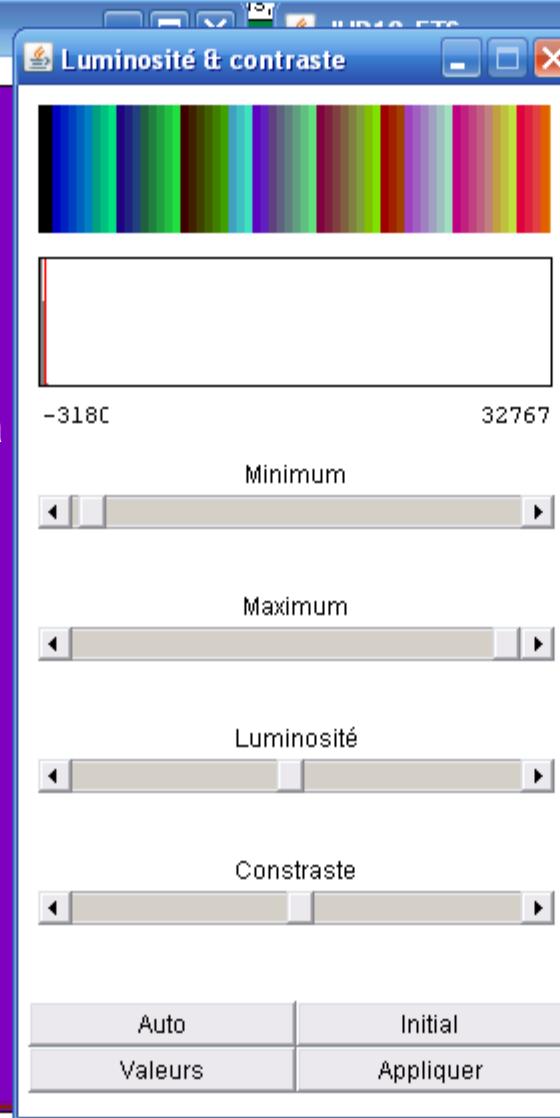
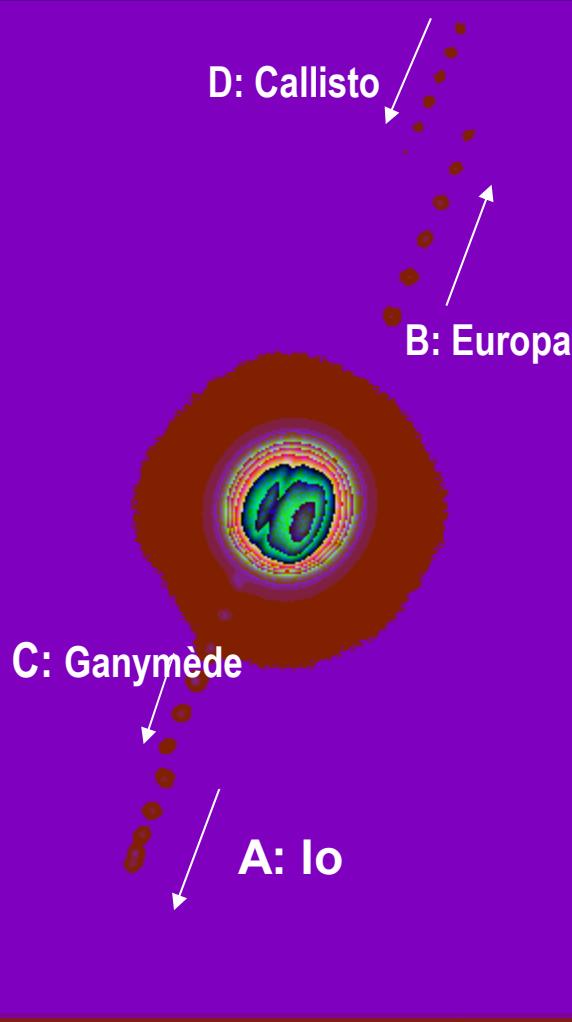
Fichier Edition Image Opérations Analyse Plugins Fenêtres Aide



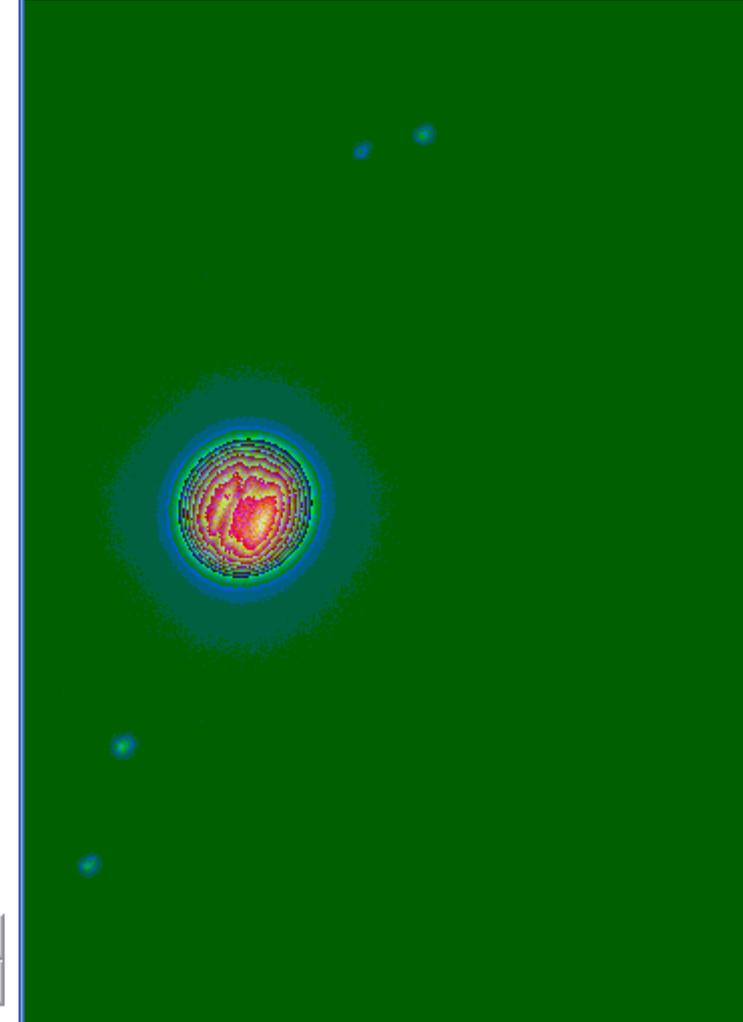
x=299, y=233, valeur=255.00 (33023)

sultat

uits Niv. de gris; 512K



uits Niv. de gris; 512K



## With SalsaJ and Galilean Moons:

- 1 – You have 5 calibrated images (date 23/4/92, one hour exactly between each image, see image information)
- 2 – Jupiter is at center coordinates (216; 216)
- 3 – On picture number 10, the moon Io is at distance R from center of Jupiter

### So, you can measure and calculate :

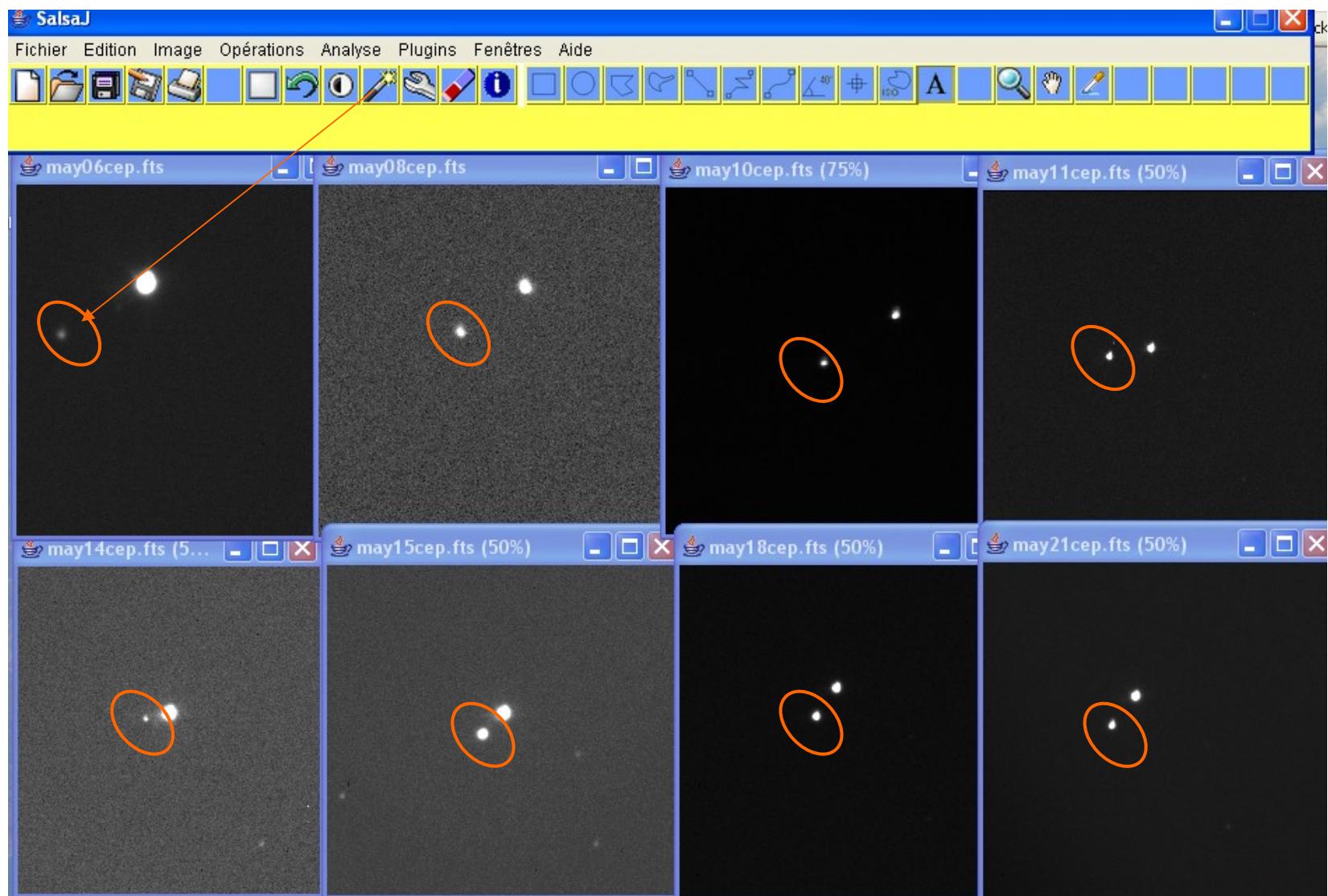
- 1 – Orbital period of Io :  $T = 1,8$  day
- 2 – Orbital radius of Io :  $R = 4,2 \cdot 10^8$  m
- 3 – Jupiter Mass:  $M_J = 4\pi^2 r^3 / G T^2 = 2 \cdot 10^{27}$  kg

Name	Discovery Date	Discoverer	Distance from Jupiter ( $10^3$ km)	Orbital Period (days)	Mass ( $10^{20}$ kg)	Radius (km)
Io (A)	1610	Galileo Galilei	421.6	1.769138	893.2	1821.6
Europa (B)			670.9	3.551181	480.0	1560.8
Ganymede (C)			1070.4	7.154553	1481.9	2631.2
Callisto (D)			1882.7	16.689018	1075.9	2410.3

# Cepheids and photometry

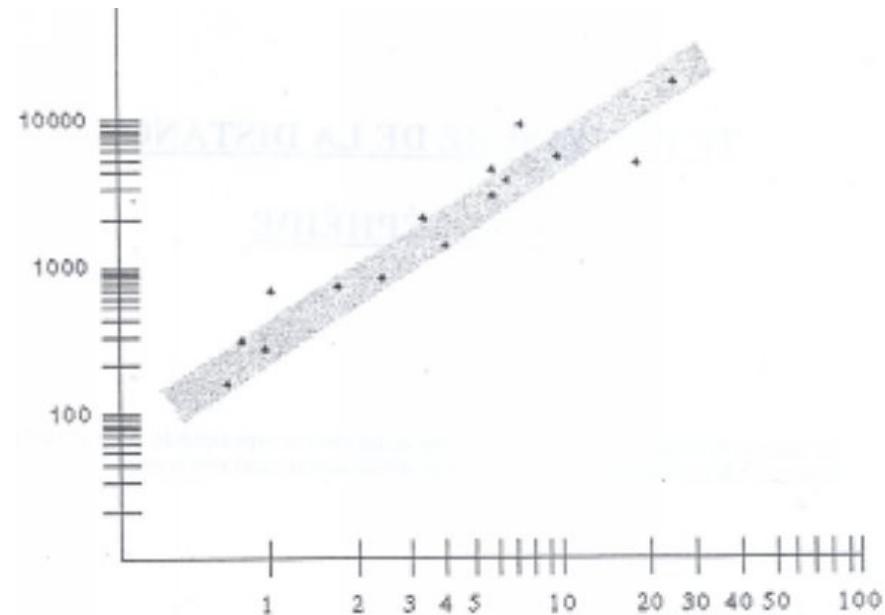
Analyse/ Photometry

Calculate the rate of brightness:  
Variable star/steady star



# Photometry of cepheids, relation *Brightness - period*

Variation périodique de l'éclat apparent de la céphéide:



Luminosité – Période: courbe établie par Henrietta Lewitt (1912)  
échelle logarithmique

$$d = (L_{\text{moy}} / 4\pi E_{\text{moy}})^{1/2} = [\text{Puissance émise par l'étoile} / (4\pi \text{Puissance reçue par unité de surface, obtenue par comparaison avec étoile de référence, voir TP})]^{1/2}$$

# Today deep sky: Captain Hooked, Hooked galaxy and a supernova

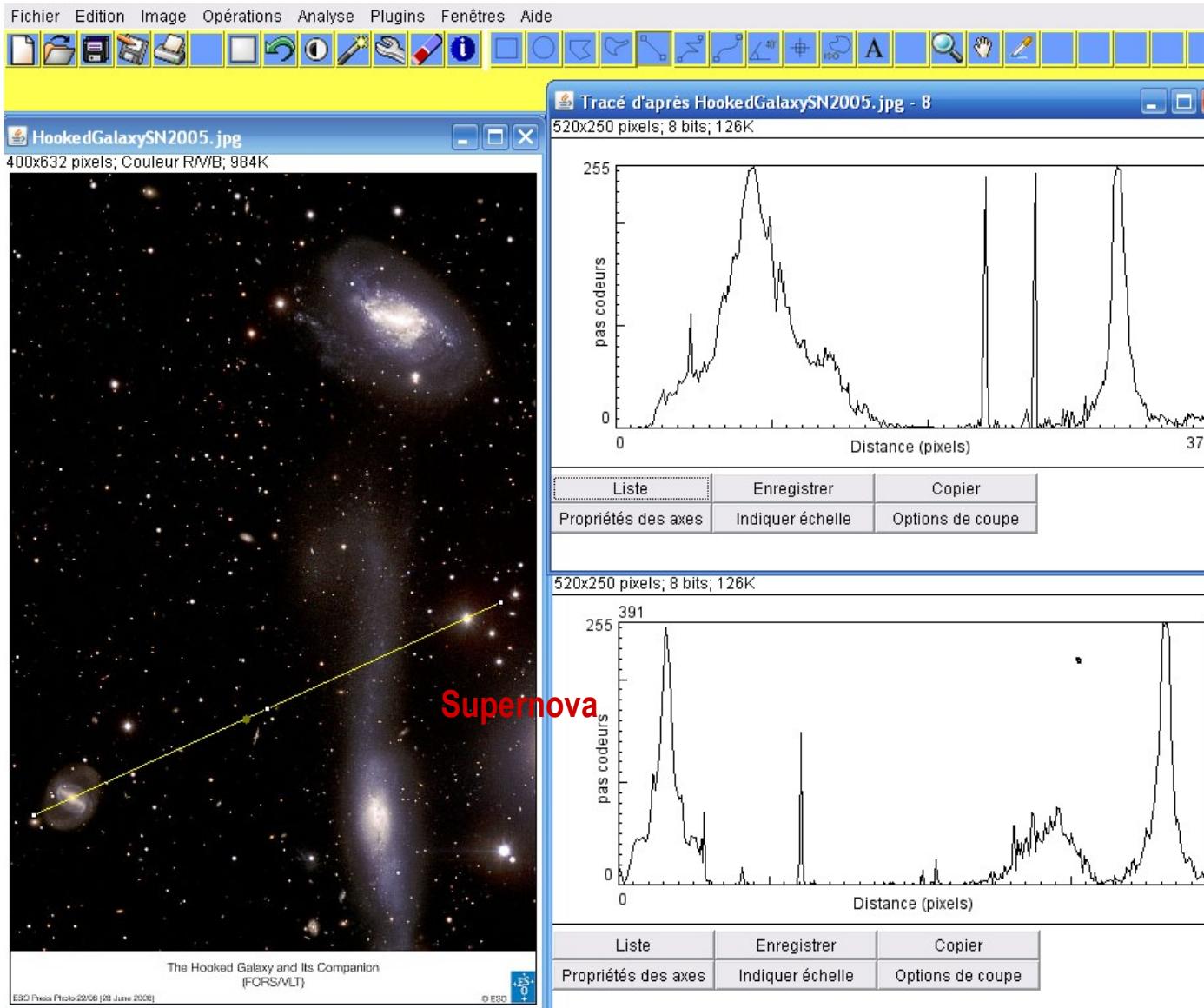
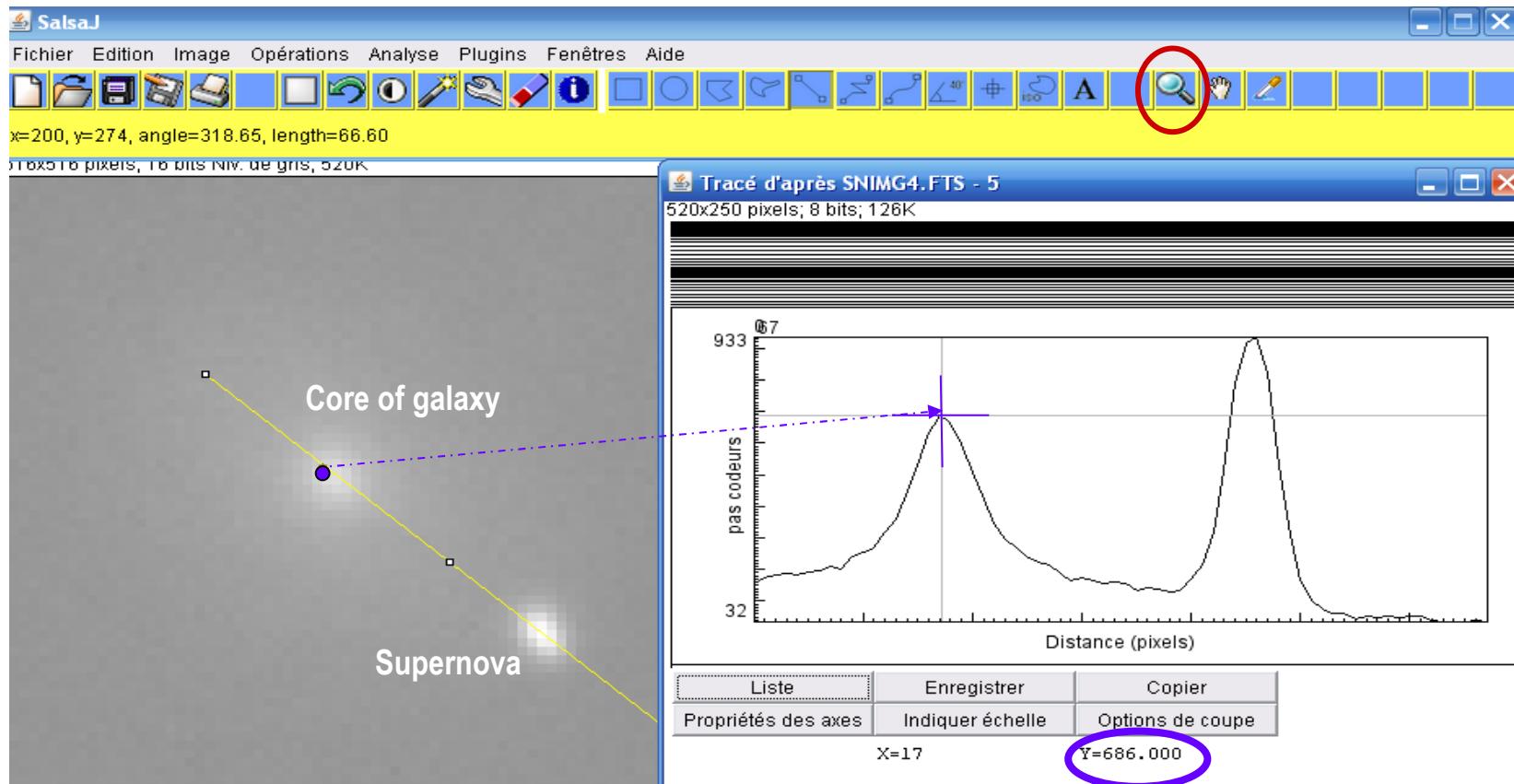


Image available on <http://www.eso.org/public/outreach/press-rel/pr-2006/images/phot-22-06-preview.jpg>

1-Open images SUPERNOVA\_LIGHT\_CURVES (12 images/ Read dates in Image Info)

2-Automatic photometry is not very precise; **open image one by one, enlarge (zoom)**

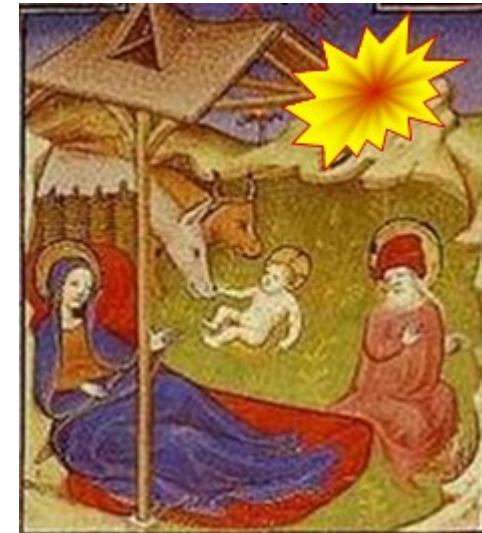
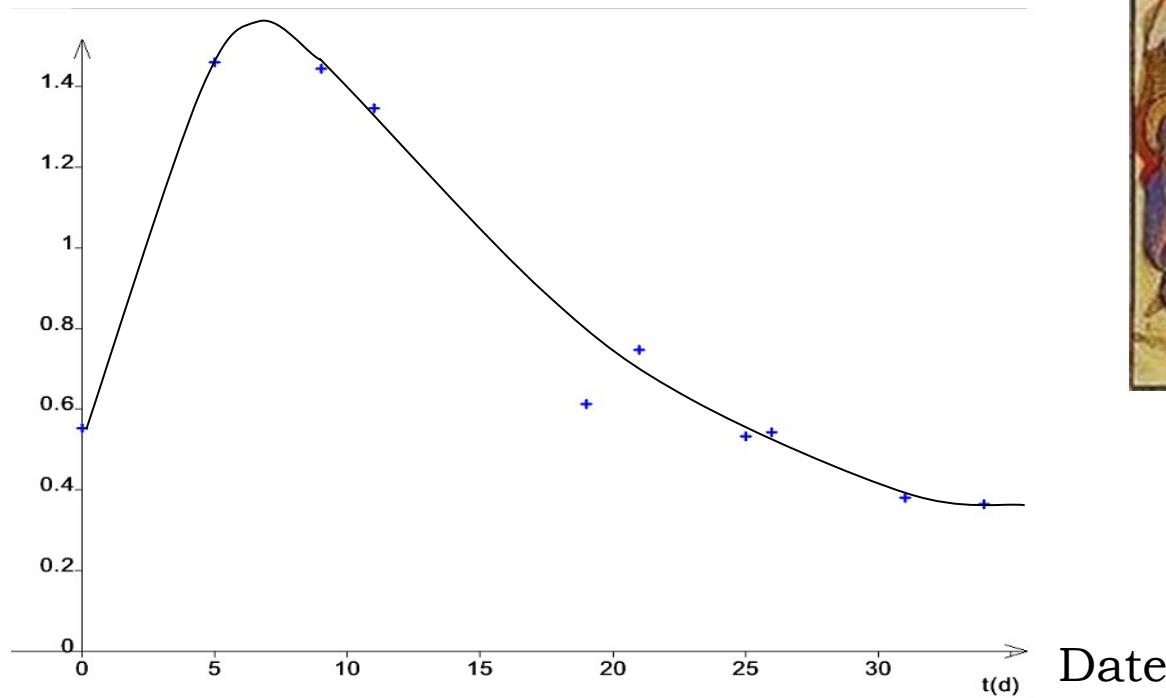
3-Use **Analyse /Plot Profile**, follow curve with cursor, then read **peaks ordinates** on each image:



Date (Image Info)	0	5	9	11	12	19	20	21	25	26	31	34
Core of galaxy	393	561	1457	686	765	1117	1116	1181	1237	1060	916	1115
Supernova	217	819	2103	923	823	665	913	883	658	576	349	407
Supernova/Core	0.552	1.460	1.443	1.345	1.076	0.595	0.818	0.748	0.532	0.543	0.381	0.365

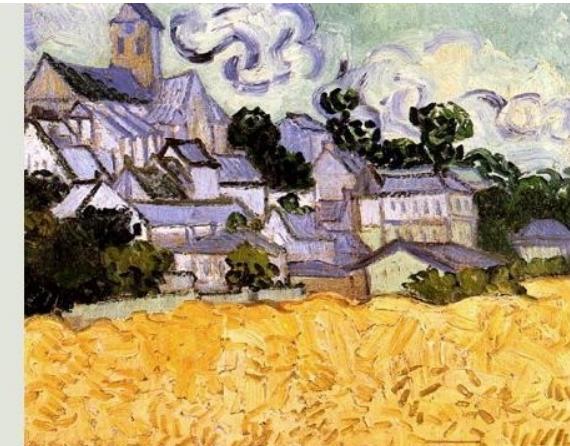
# Draw the curve of supernova brightness (calculated with reference to galaxy core) according to date

Supernova Brightness/ Galaxy core

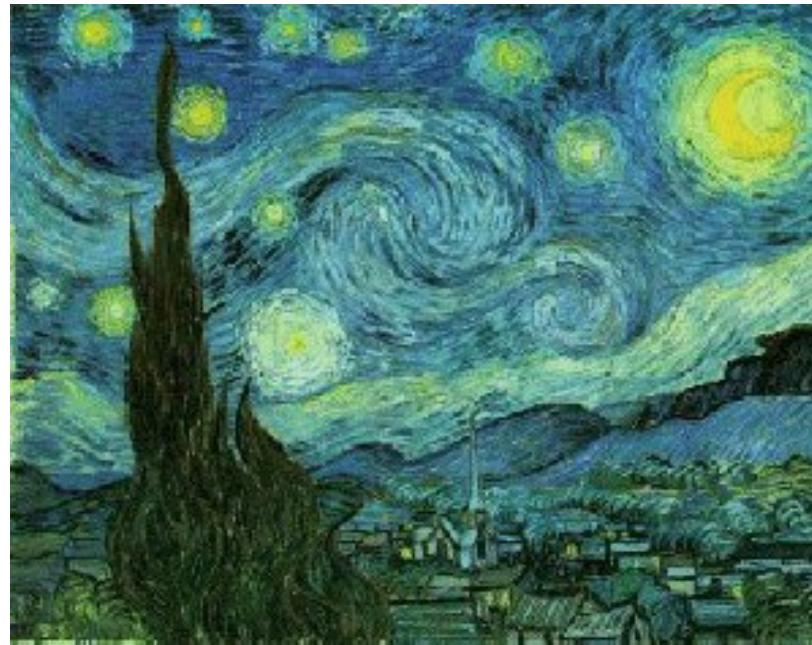


Supernovae are used as cosmic candles for measuring distances in the Universe.

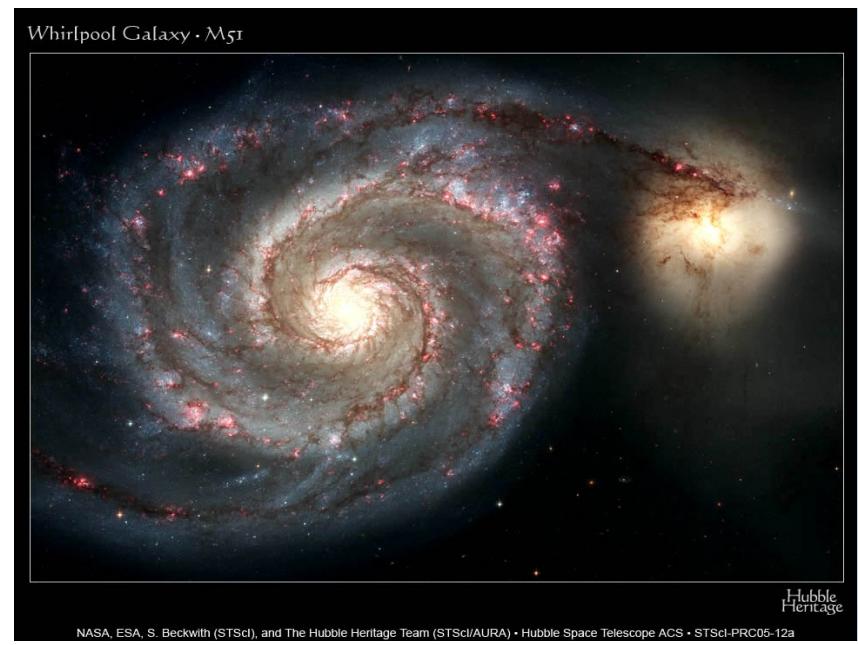
5th step : Galaxies with Van Gogh  
in Auvers-sur-Oise  
a village near Paris



*Auvers-sur-Oise, by Van Gogh*



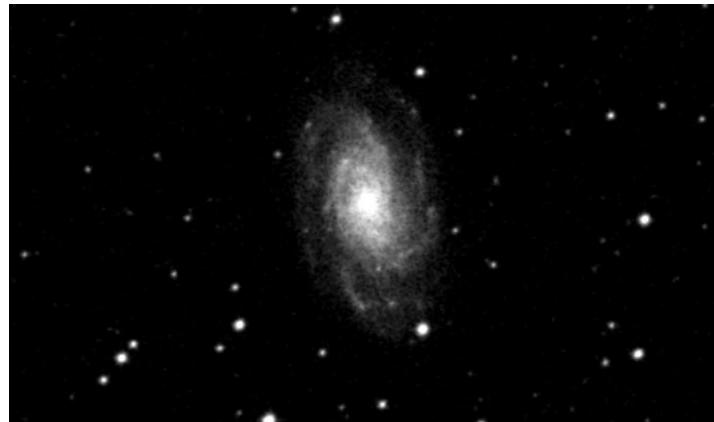
*Starry night, by Vincent Van Gogh*



M51, Whirlpool Galaxy(english whirlpool= french tourbillon)

# Dancing with a galaxy

## About galaxy NGC 7083, redshift and dark matter



Measuring *Edwin Hubble's redshift* and *Vera Rubin's dark matter*



Education and Culture

Socrates  
Minerva



Global HOU – Lisbon 2008

Suzanne FAYE, Lycée Chaptal, Paris, France

Michel FAYE, Lycée Louis-le-Grand, Paris, France

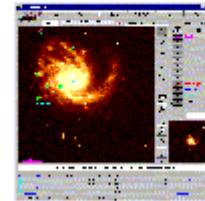
[mfaye2@wanadoo.fr](mailto:mfaye2@wanadoo.fr)

# I - About galaxy NGC 7083

Where? in Indus Constellation (Southern hemisphere)

Why Southern hemisphere? Because of very performant telescope ESO – VLT (Chili)

[Aladin Java Applet](#)



<http://seds.org/~spider/ngc/ngc.cgi?7083>

<http://simbad3.u-strabg.fr/sim-id.pl?Ident=NGC7083>

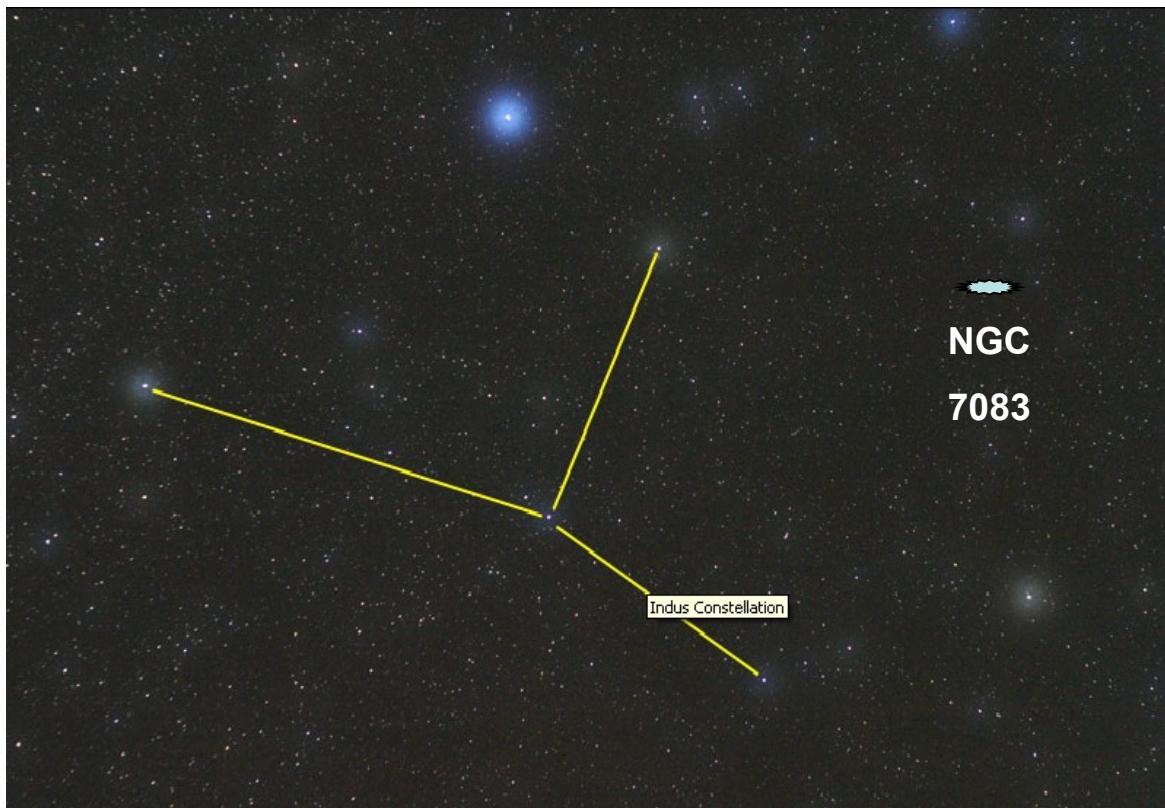
<b>Right Ascension:</b>	21 hours 35 minutes 45,4 s
<b>Declination:</b>	-63 degrees, 54 minutes 17s
<b>Apparent Magnitude:</b>	12
<b>Apparent Diameters:</b>	3.5' long; 2,0' wide (slide 4)

# 1 - About Indus Constellation, southern hemisphere (visible with VLT, Chili)

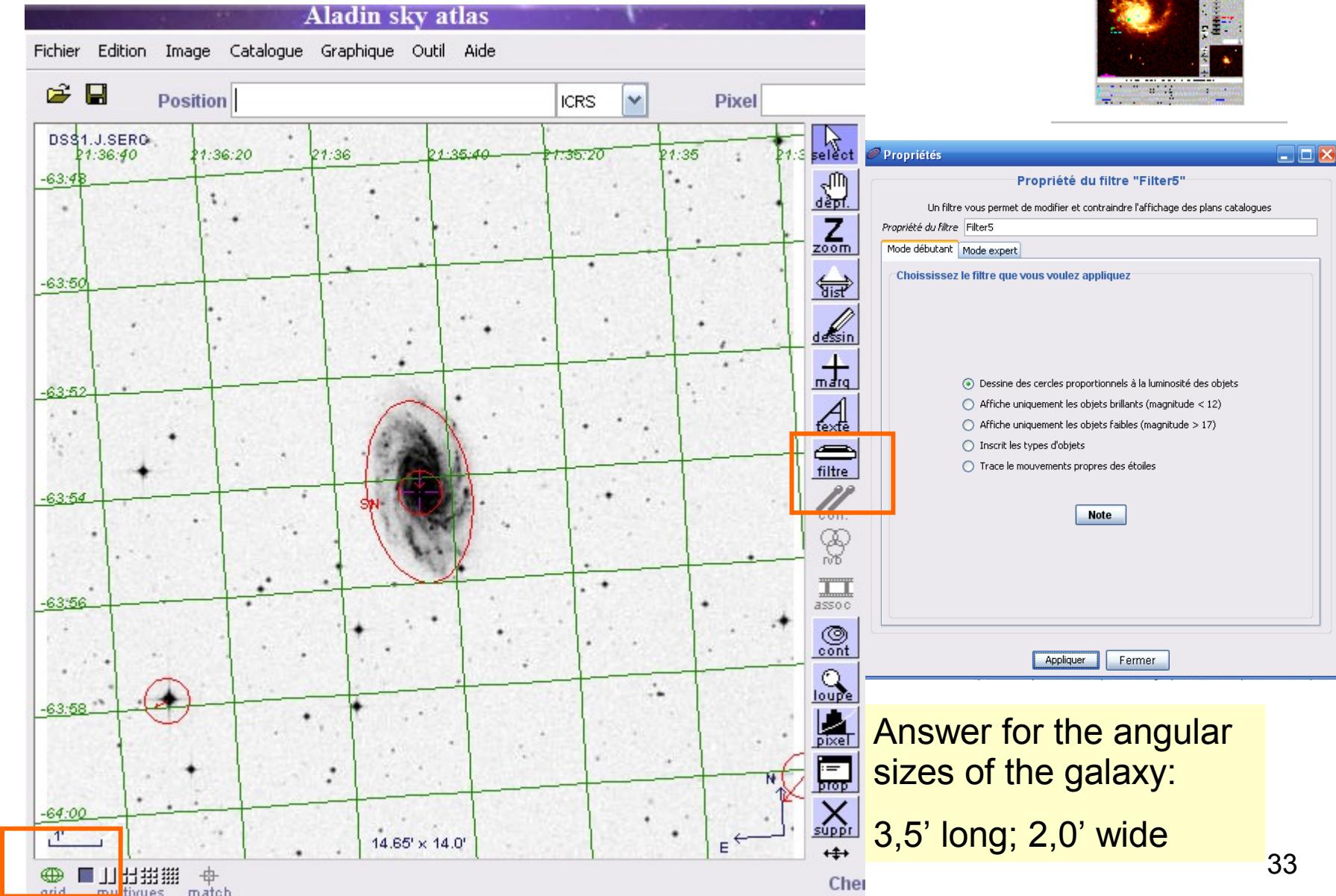
<http://www.starrynightphotos.com/constellations/indus.htm>

The constellation was one of twelve constellations created by Pieter Dirkszoon Keyser and Frederick de Houtman between 1595 and 1597, and it first appeared in Johann Bayer's *Uranometria* of 1603.

Since Indus was introduced in the 17th century, and lies in the south, it was not known to classical or early cultures thus they produced no mythology concerning it.

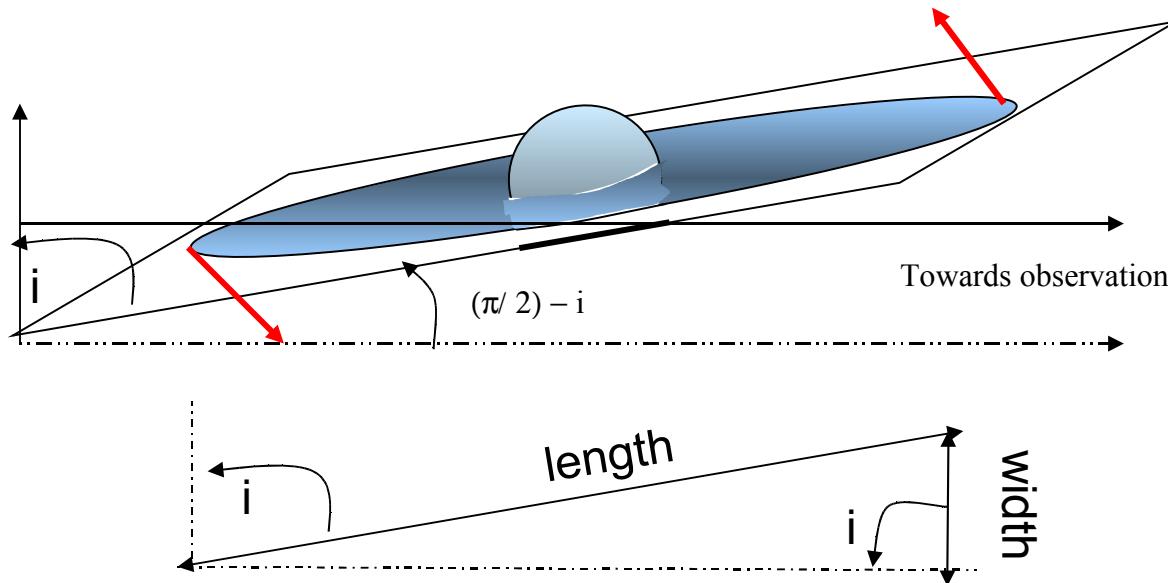


## 2 - <http://simbad3.u-strasbg.fr/sim-id.pl?Ident=NGC7083>



### 3 – What is the orientation of the galaxy disc plane; angle $i$ ?

We see as an ellipse what is in fact a circle.

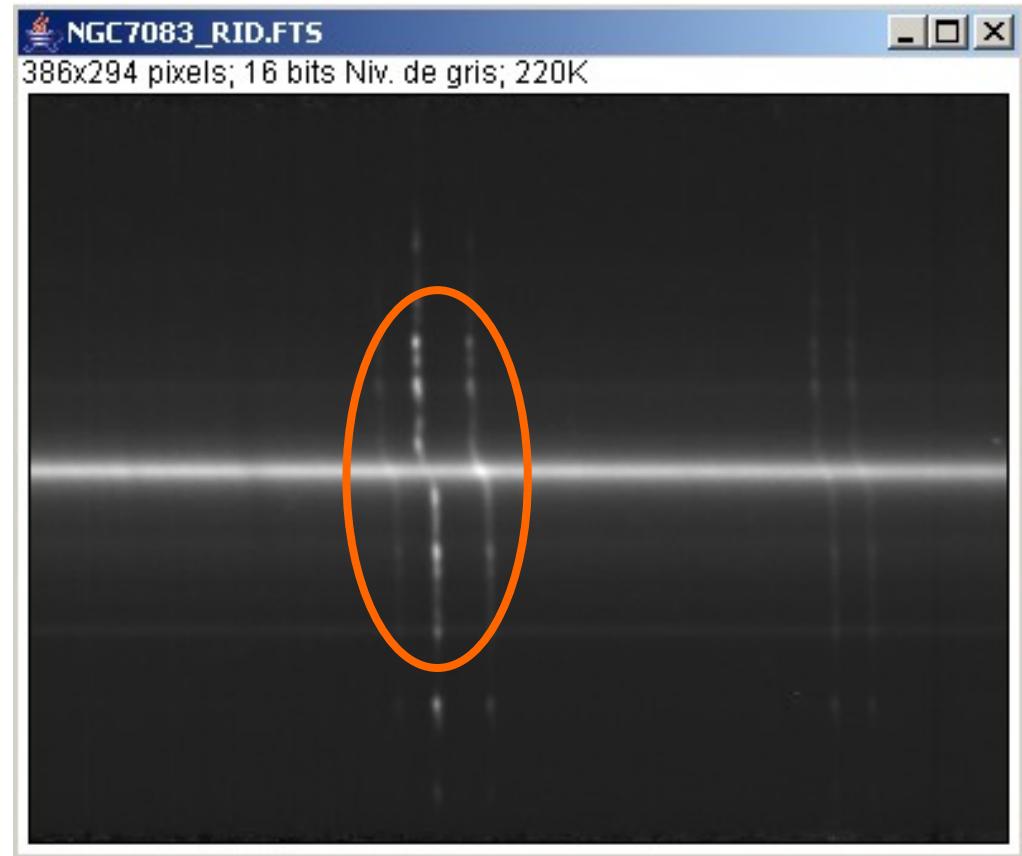
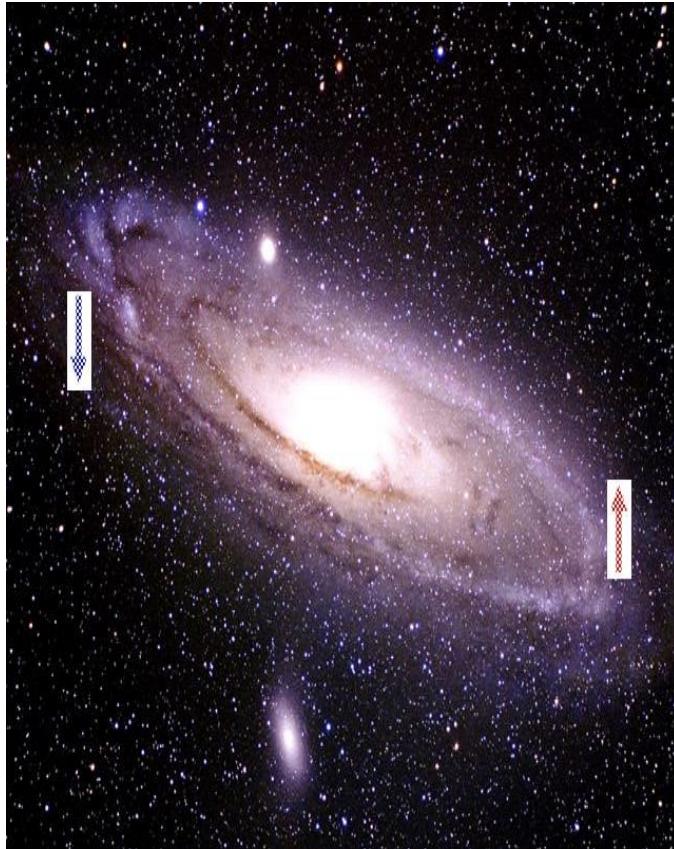
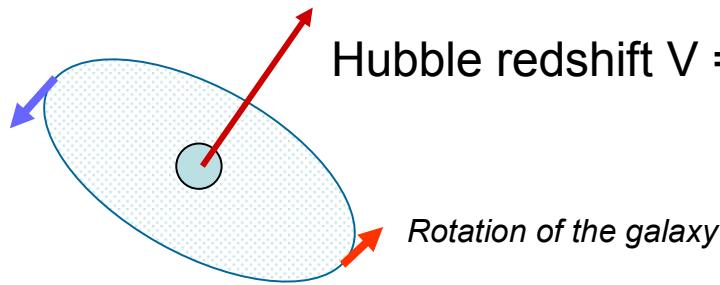


Answer for angle  $i$  :  $\cos(i) = \text{width}/\text{length} = 2,0 / 3,5 \Rightarrow i = 55^\circ$ ;  $\sin(i) = 0,82$

## Pretty Doppler effects

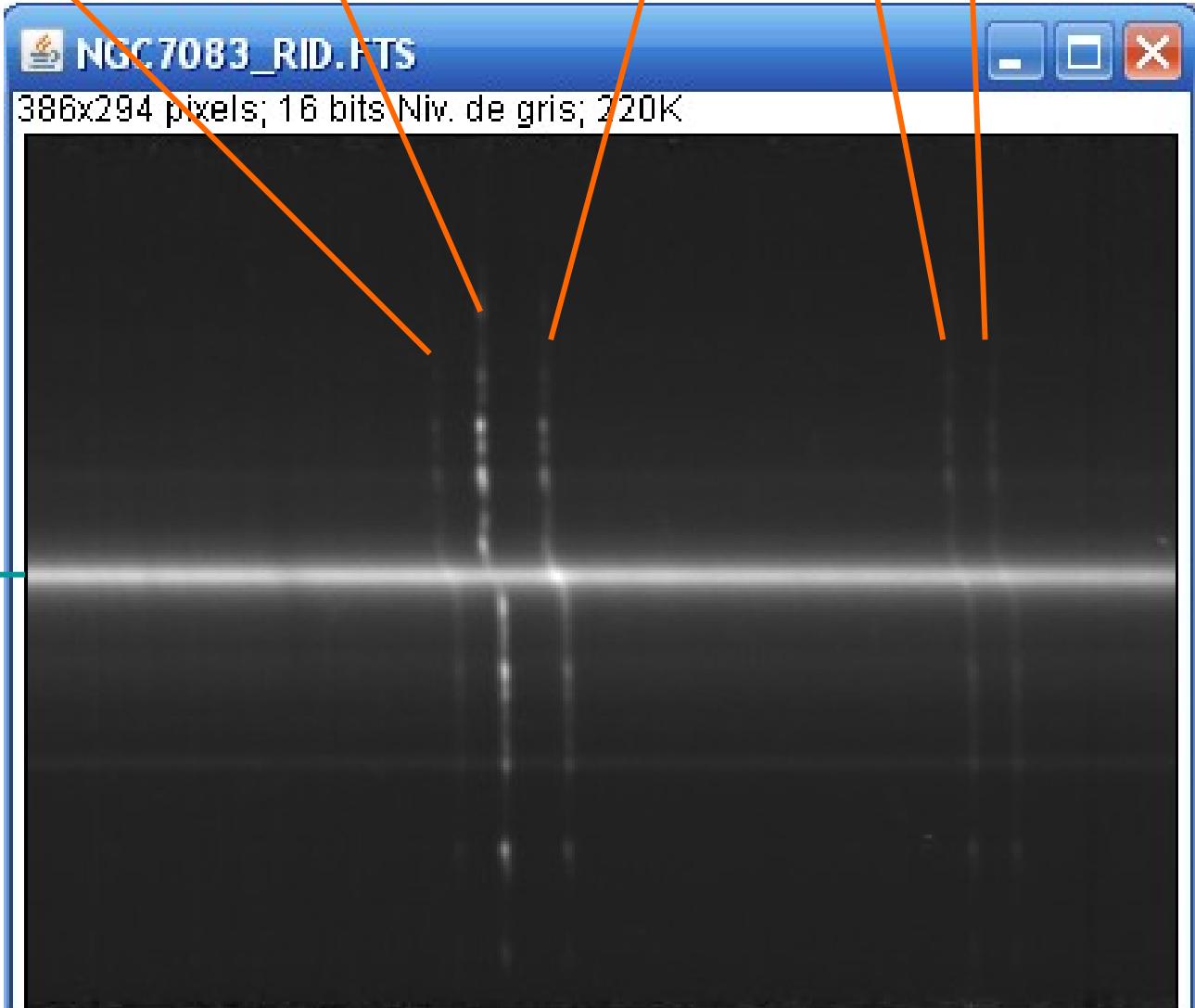
*Rotation of the galaxy*

Hubble redshift  $V = H^* D$

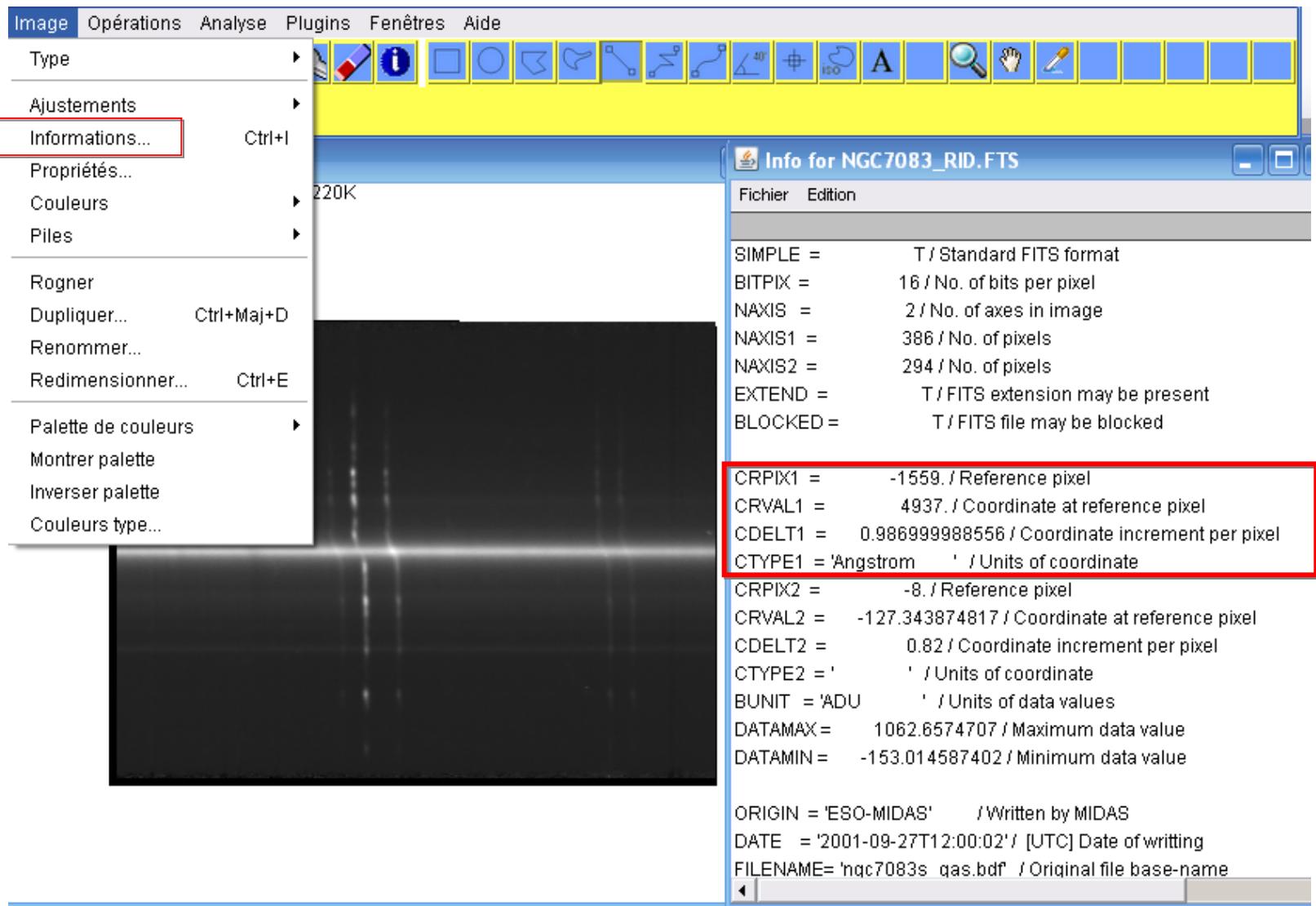


#### 4 – Part of NGC 7083 spectrum, by VLT - ESO / cf Italy: Alessandra Zanassi, Marileva Spavone

Lines emitted by atoms from the disk of the galaxy



## 5 – Have a look at Image/ Informations



## 6 – Which lines did VLT astronomers have sent to us?

N nitrogen

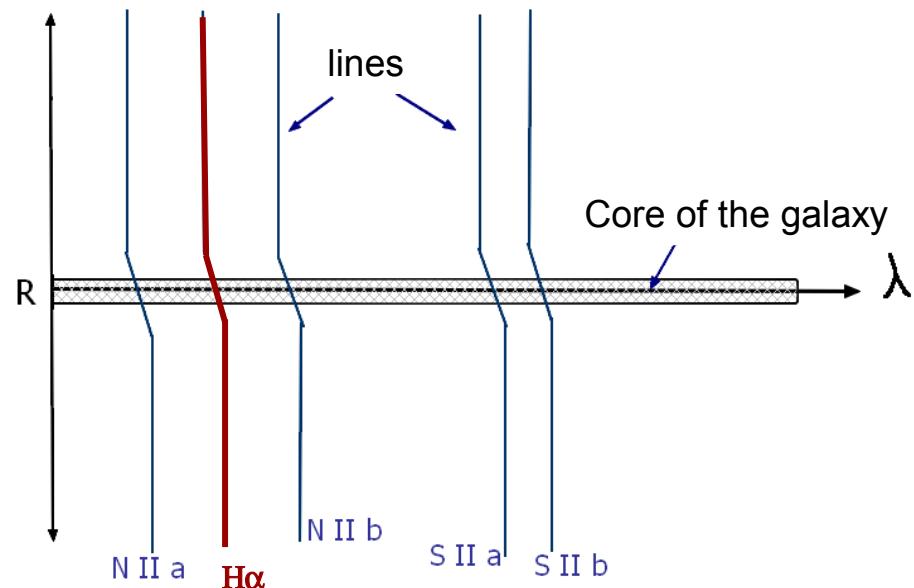
H hydrogen

S sulfur

$$\lambda(\text{pixel}) = a^*(\text{pixel-reference}) + b$$

=

$$\text{CDELT1} * (\text{pixel} + 1559) + 4937 \text{ } (\text{\AA})$$



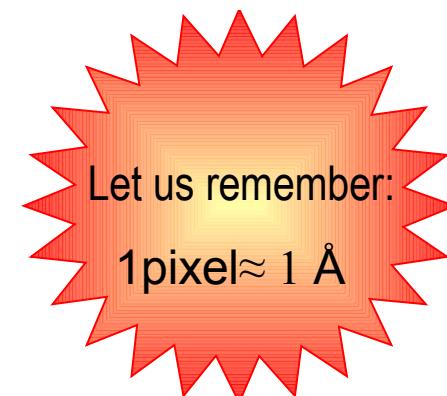
### Image Information:

CRPIX1 = -1559. / Reference pixel

CRVAL1 = 4937. / Coordinate at reference pixel

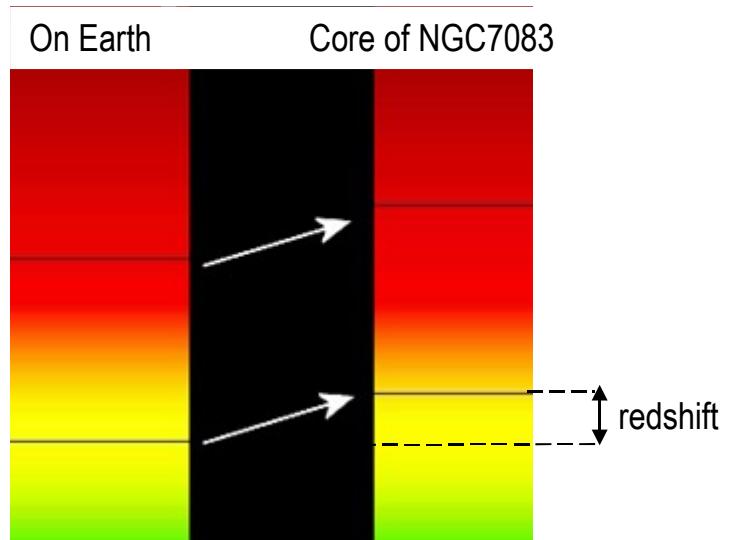
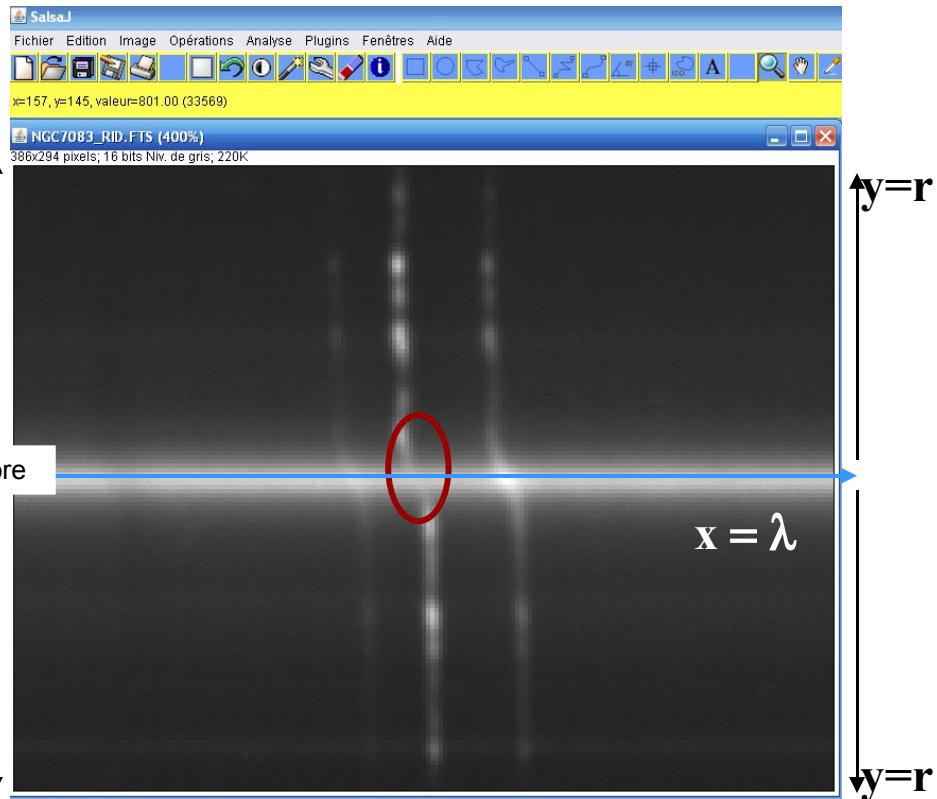
CDELT1 = 0.986999988556 / Coordinate increment per pixel

CTYPE1 = 'Angstrom' / Units of coordinate



## 7 -Spectrum of NGC 7083 - Magnifying glass

Image Information:  $\lambda_{\text{nm}} = (X + 1559) \cdot 0,0987 + 493,7$



$$\begin{aligned} \text{Raie H}\alpha : X &= 156 \\ \text{So } \lambda &= (156 + 1559) \times \\ &0,0987 + 493,7 \\ \lambda &= 663,0 \text{ nm} \end{aligned}$$

Line	Spectrum on Earth $\lambda_1$ (nm)	Spectrum of NGC 7083 $X$ (pixel) => $\lambda_2$ (nm)	Redshift $\Delta\lambda/\lambda = (\lambda_2 - \lambda_1) / \lambda_1$	$V_{\text{galaxie}} = c \cdot \Delta\lambda/\lambda$ (km/s) $c = 3 \cdot 10^5 \text{ km/s}$
Hα	656.28	$X = 156 ;$ $\lambda_2 = 663.0$	0.0102	3060

## 8 – Calculate redshift for each line

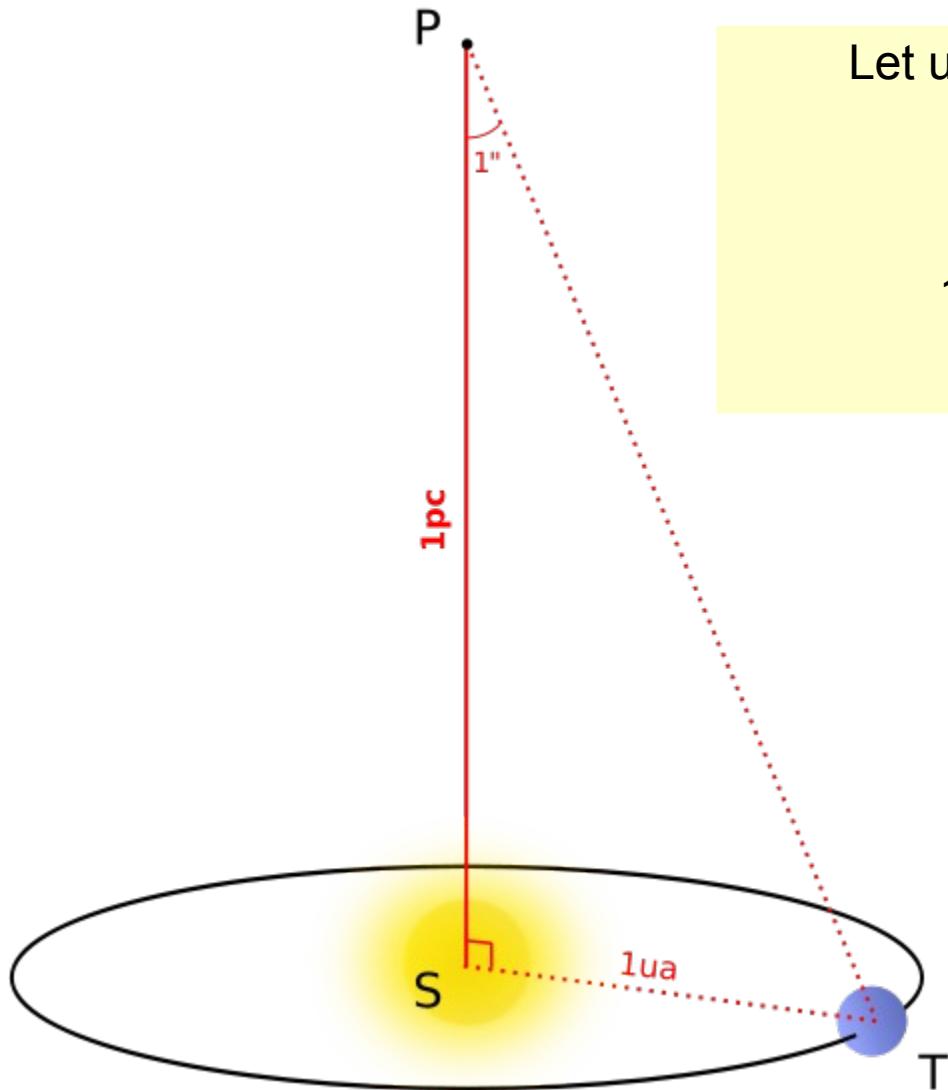
$$\lambda(\text{pixel}) = a * (\text{pixel}-\text{reference}) + b = \text{CDELT1} * (\text{pixel} + 1559) + 4937 \text{ } (\text{\AA})$$

Line	Spectrum on Earth $\lambda_1$ (nm)	Spectrum of NGC 7083 X (pixel) => $\lambda_2$ (nm)		Redshift $\Delta\lambda/\lambda = (\lambda_2 - \lambda_1) / \lambda_1$	$V_{\text{galaxie}} = c \cdot \Delta\lambda/\lambda$ (km/s) $c = 3 \cdot 10^5 \text{ km/s}$
NIIa	654.80	X=140	$\lambda_2 = 661.6$	0.0103	3090
<b>H<math>\alpha</math></b>	<b>656.28</b>	<b>X=156</b>	<b><math>\lambda_2 = 663.0</math></b>	<b>0.0102</b>	<b>3060</b>
NIIb	658.35	X=178	$\lambda_2 = 665.2$	0.0104	3120
SIIa	671.60	X=313	$\lambda_2 = 678.6$	0.0104	3120
SIIb	673.10	X=328	$\lambda_2 = 680.0$	0.0102	3060

Let us keep  $V_{\text{NGC7083}} = 3.09 \cdot 10^3 \text{ km/s}$

Good measurement!

## 9 – What is the distance D of galaxy NGC 7083?



Let us use Hubble law :  $V_{\text{galaxie}} = H * D$  ,  
with  $H \approx 73 \text{ km.s}^{-1}.\text{Mpc}^{-1}$

$$1\text{pc} = 3,26 \text{ a.l. et } 1\text{a.l.} \approx 9,47 \cdot 10^{15} \text{ m}$$

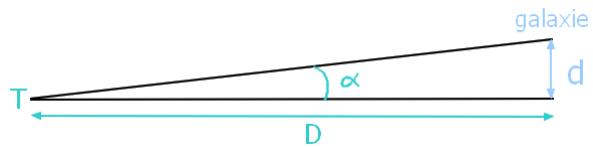
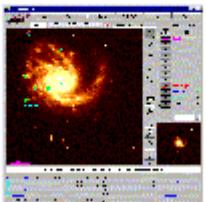
$$\begin{aligned}D &= V_{\text{NGC7083}} / H = 3090 / 73 \\&= 42,3 \text{ Mpc} = 4,23 \times 10^7 \text{ pc}\end{aligned}$$

$$D = 13,8 \times 10^7 \text{ a.l.}$$

$$D = 1,31 \times 10^{24} \text{ m}$$

## 10 - Measuring the size $d_{\text{NGC7083}}$ of the galaxy

[Aladin Java Applet](#)



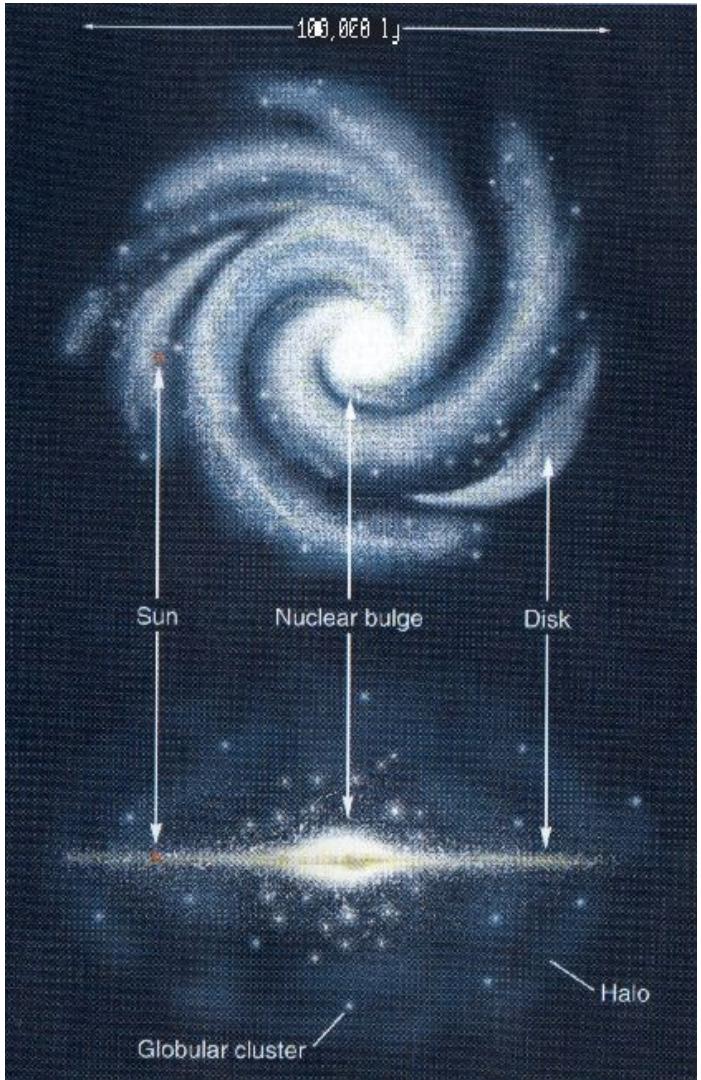
$$d_{\text{galaxy}} = \alpha(\text{en radians}) * D$$

$$\alpha_{\text{NGC 7083}} \approx 3,5' = 1,02 \cdot 10^{-3} \text{ rad}$$

$$D = 4,23 \times 10^7 \text{ pc}$$

Our Galaxy, Milky Way :  $d_{\text{Milky Way}} = 25 \ 000 \text{ pc}$

NGC 7083:  $d_{\text{NGC7083}} = 4,3 \cdot 10^4 \text{ pc} = 1,7 * d_{\text{Milky Way}}$



## 11 – Have sizes of the galaxy with Image/ Informations and apparent diameters

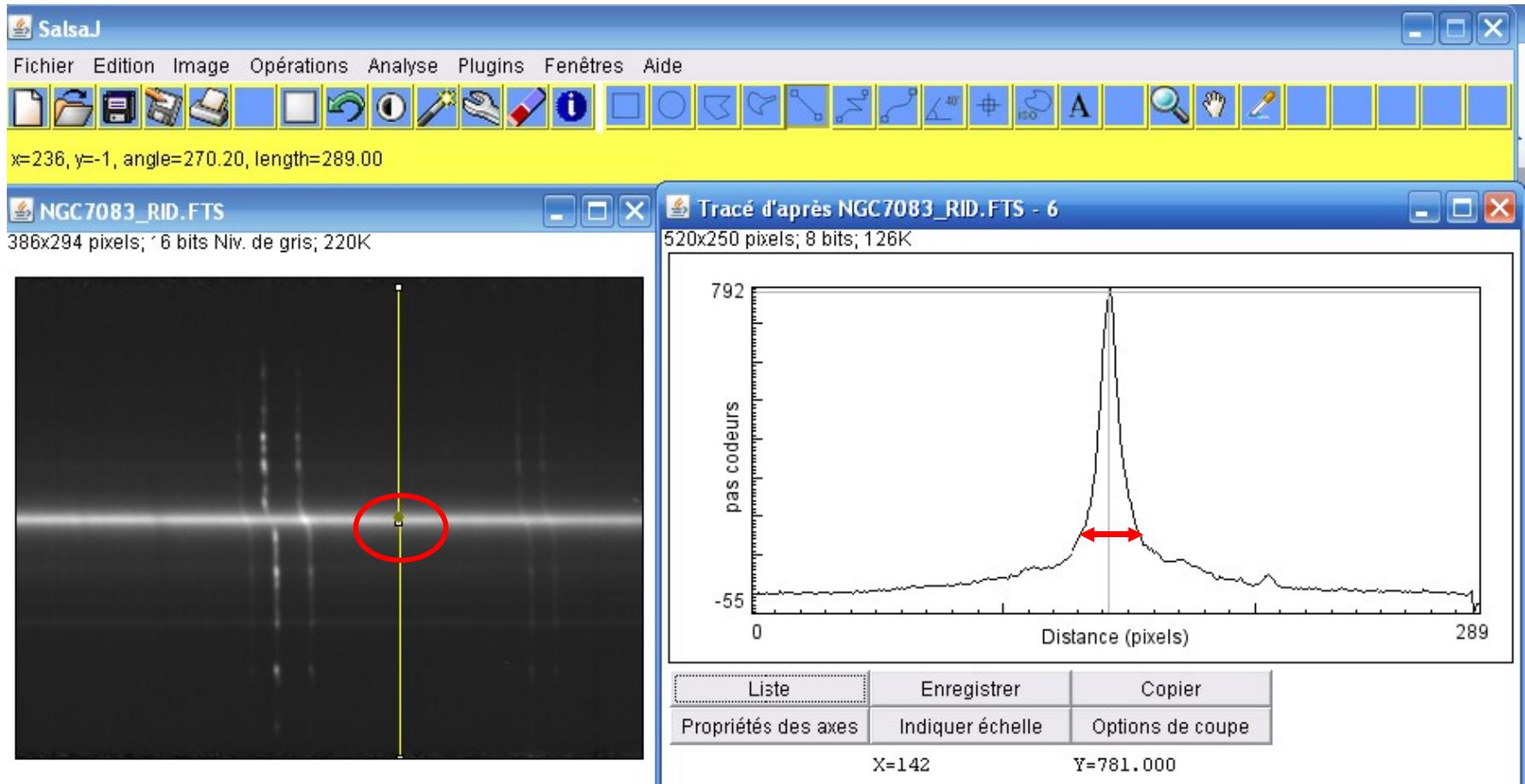
The screenshot shows a software interface for astronomical image processing. On the left, a vertical menu is open under the "Image" tab, containing options like "Type", "Ajustements", "Informations...", "Propriétés...", "Couleurs", "Piles", "Rogner", "Dupliquer...", "Renommer...", "Redimensionner...", "Palette de couleurs", "Montrer palette", "Inverser palette", and "Couleurs type...". A blue arrow points from the "Informations..." option in the menu down to the "Info for NGC7083\_RID.FTS" dialog box. Another blue arrow points from the bottom of the dialog box back up to the "Informations..." option in the menu. The dialog box itself has a title bar "Info for NGC7083\_RID.FTS" and a menu bar with "Fichier" and "Edition". It lists various FITS header parameters:

SIMPLE =	T / Standard FITS format
BITPIX =	16 / No. of bits per pixel
NAXIS =	2 / No. of axes in image
NAXIS1 =	386 / No. of pixels
NAXIS2 =	294 / No. of pixels
EXTEND =	T / FITS extension may be present
BLOCKED =	T / FITS file may be blocked
CRPIX1 =	-1559. / Reference pixel
CRVAL1 =	4937. / Coordinate at reference pixel
CDELT1 =	0.986999988556 / Coordinate increment per pixel
CTYPE1 =	'Angstrom' / Units of coordinate
CRPIX2 =	-8. / Reference pixel
CRVAL2 =	-127.343874817 / Coordinate at reference pixel
CDELT2 =	0.82 / Coordinate increment per pixel
CTYPE2 =	' ' / Units of coordinate
BUNIT =	'ADU' / Units of data values
DATAMAX =	1062.6574707 / Maximum data value
DATAMIN =	-153.014587402 / Minimum data value
ORIGIN =	'ESO-MIDAS' / Written by MIDAS
DATE =	'2001-09-27T12:00:02' / [UTC] Date of writing
FILENAME=	'hqc7083s_qas.bdf' / Original file base-name

On the left side of the main window, there is a preview of the astronomical image showing a central bright region (the galaxy core) and surrounding diffuse light. A blue oval highlights the central core area. Below the preview, three pieces of text are displayed in a light blue box:

- $\alpha_{\text{core}} \approx 16 \text{ pixels} = 13''$
- Width of the picture  $\approx 289 \text{ pixels} = 237''$
- $\alpha_{\text{NGC 7083}} \approx 3.5' = 210'' = 256 \text{ pixels}$

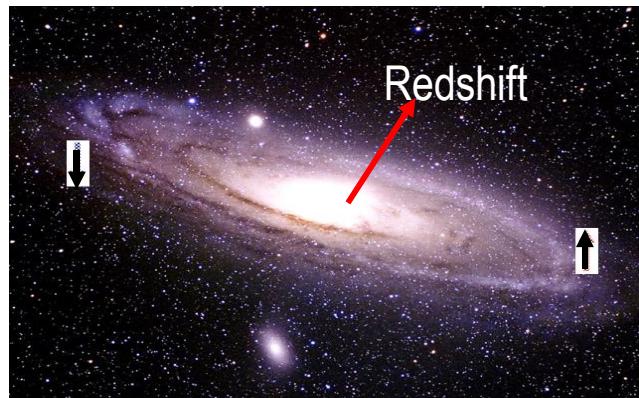
## 12 – Measuring the size $d_{\text{core}}$ of the core of the galaxy : « vertical » slice



Let us evaluate: core = 16 pixels;  $d_{\text{NGC7083}} \approx 256$  pixels

$$\Rightarrow d_{\text{core}} / d_{\text{galaxy}} = 16/256 \text{ et } d_{\text{NGC7083}} = 4,3 \cdot 10^4 \text{ pc} ; \text{ so } d_{\text{core}} \approx 2,7 \cdot 10^3 \text{ pc} = 8,3 \cdot 10^{19} \text{ m}$$

# II – Dancing with a galaxy



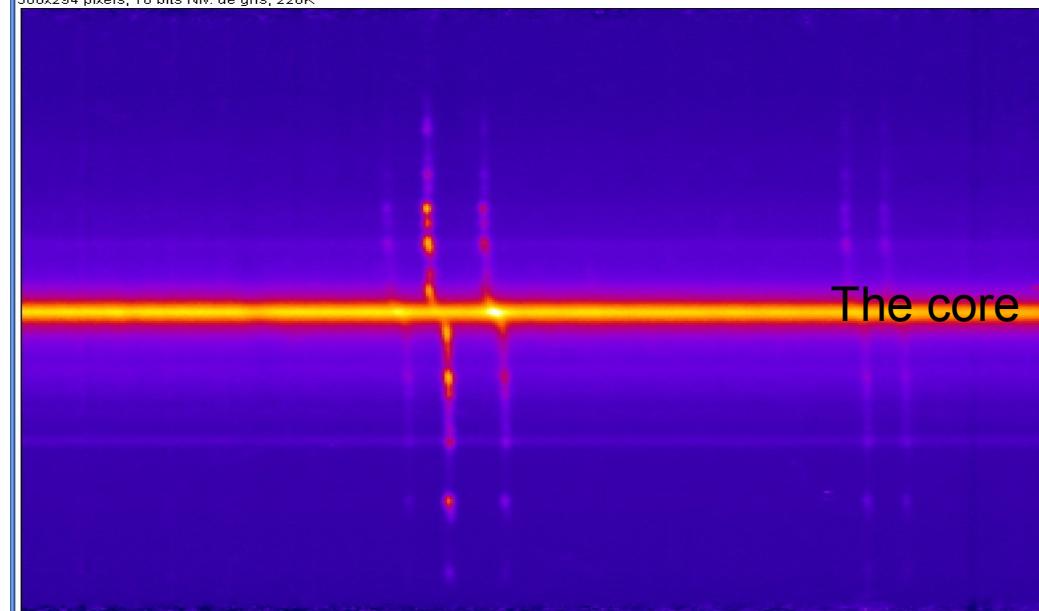
Redshift of the core

+

« Relative » Doppler shift by rotating around the core

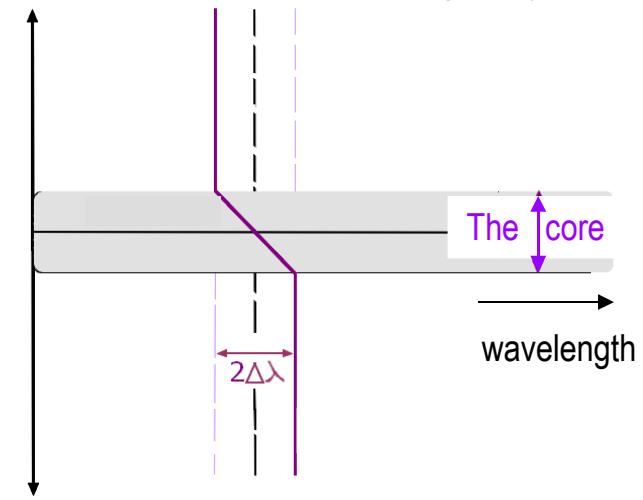


NGC 7083\_RID.FTS (200%)  
386x294 pixels; 16 bits Niv. de gris; 220K



The core

$r$ , distance to the core of the galaxy

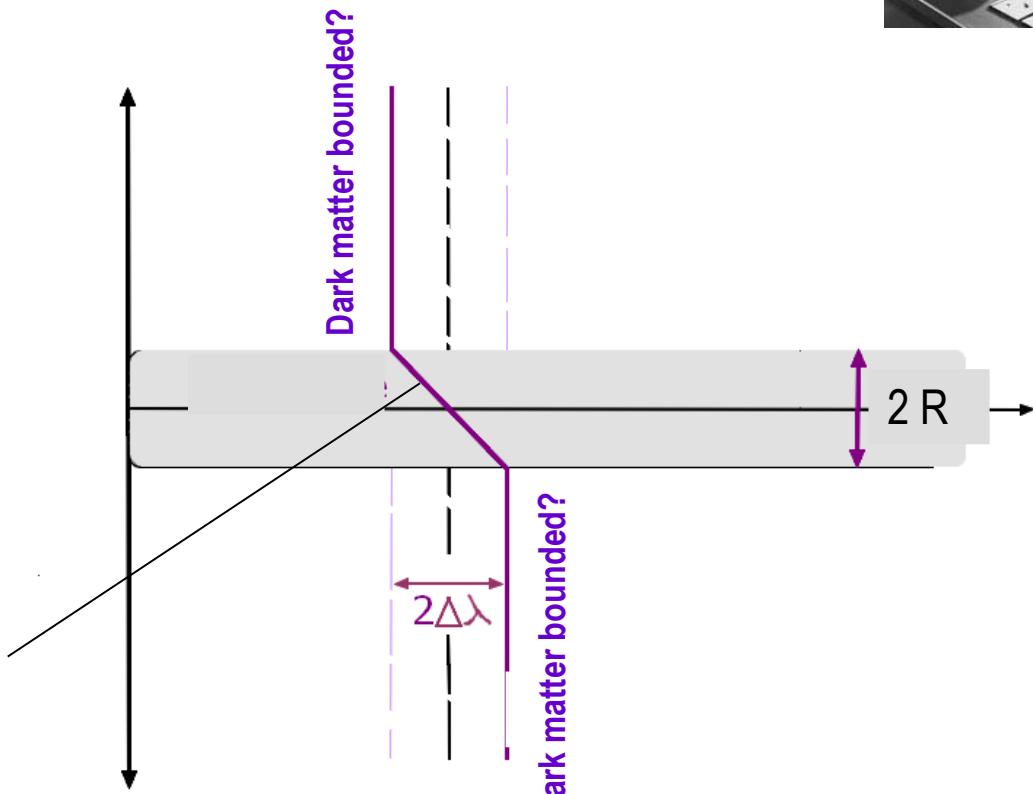


# 1 – Why is the shift of the spectrum constant for $r > R$ ?

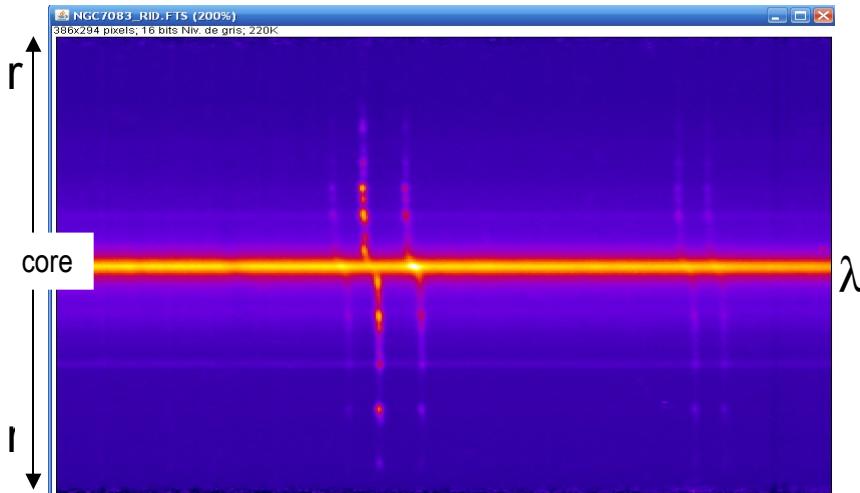
**Vera Rubin** (born 1928) is an astronomer who has done pioneering work on galaxy rotation rates. Her discovery of what is known as "flat rotation curves" is the most direct and robust evidence of **dark matter**.



Turning around  
the core



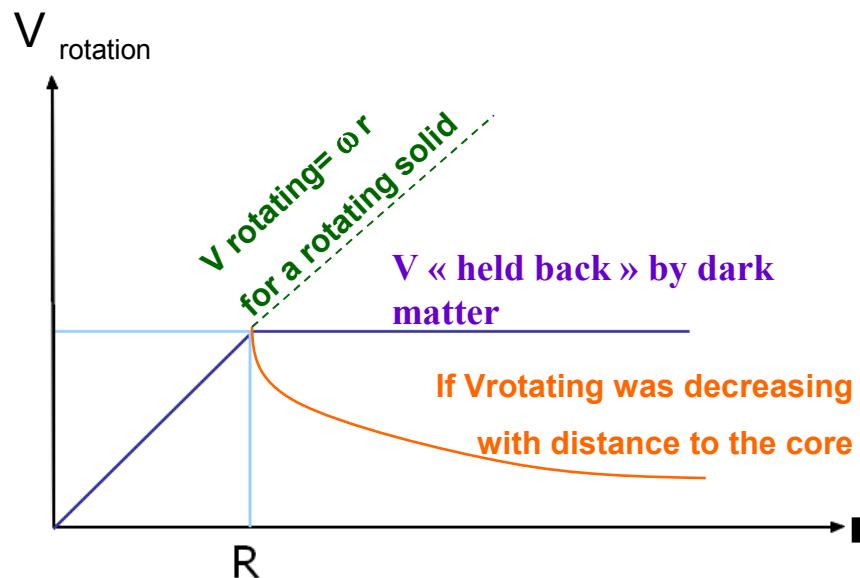
## Danse with a galaxy / Dark matter



Let us imagine that  
the arms of the  
dancer are «held  
back» by ???

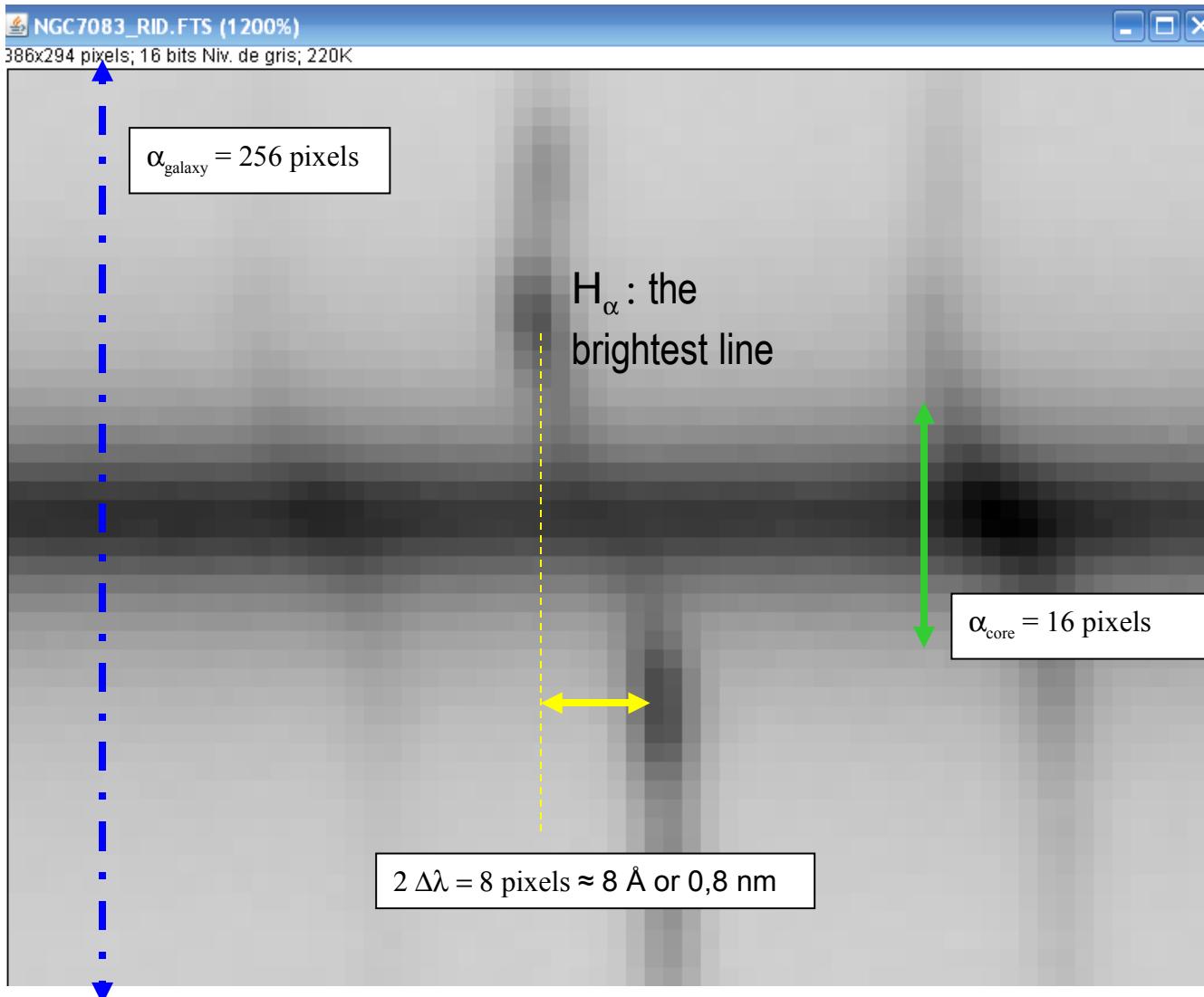
**Dark Matter!!!**

- \* Doppler shift  $\Delta\lambda$  is constant for  $r > R$ , which means that the relative velocity is then constant
- \* Because of the inclination  $i$  of the galaxy plane,  $\Delta\lambda / \lambda = V_{\text{relative}} * \sin(i) / c$



### 3 – How can we measure $\Delta\lambda / \lambda$ ?

You can either use quotient in pixel, or use CDELT1: 1 pixel  $\approx 1 \text{ \AA}$  or  $0,1 \text{ nm}$



$$V_{\text{rotation}} = [\Delta\lambda/\lambda] * c / \sin(55)$$

We use line  $H_{\alpha}$ ,  
with rotation shift

$$\lambda(H_{\alpha}/\text{core}) \approx 6630 \text{ \AA}$$

So:

$$V_{\text{rotation}} \approx (4/6630) * c/0.82$$

$$V_{\text{rotation}} \approx 2,21 \cdot 10^5 \text{ m/s}$$

Around the core of the galaxy:

$$mV^2 / r = G m M / r^2$$

$$\text{so } M_{\text{core}} = V^2 R / G$$

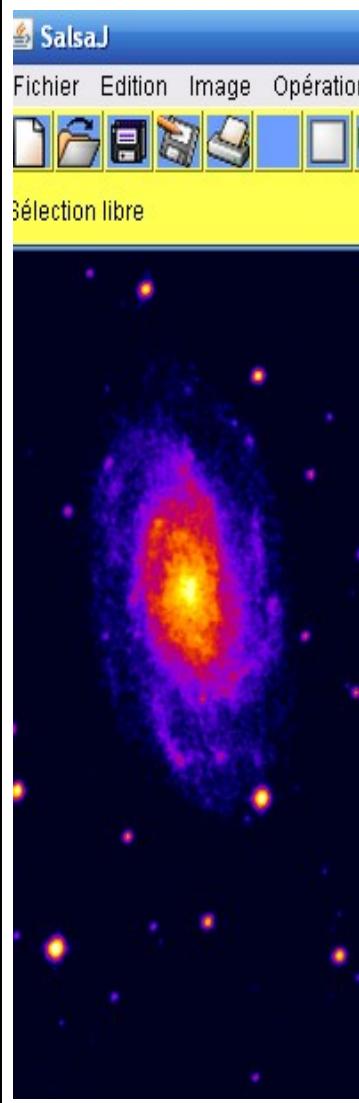
$$G = 6,67 \cdot 10^{-11} \text{ SI}$$

$$R = d_{\text{core}}/2 \quad 4,15 \cdot 10^{19} \text{ m}$$

$$M_{\text{core}} = 3 \cdot 10^{40} \text{ kg}$$

Simpler:

$$\begin{aligned} \text{Total Mass / Visible Mass} &= \\ 256/16 &= 16 \quad 48 \end{aligned}$$



**For the core of the galaxy:**

$$mV^2 / R = G m M_{\text{core}} / R^2$$

$$\text{so } M_{\text{core}} = V^2 R / G$$

$$G = 6,67 \cdot 10^{-11} \text{ SI}$$

$$R = d_{\text{core}}/2 \approx 4,15 \cdot 10^{19} \text{ m}$$

$$M_{\text{core}} = 3 \cdot 10^{40} \text{ kg}$$

**For the whole galaxy:**

$$mV^2 / r_{\text{whole}} = G m M_{\text{whole}} / r_{\text{whole}}^2$$

$$\text{so } M_{\text{whole}} = V^2 r_{\text{whole}} / G$$

$$G = 6,67 \cdot 10^{-11} \text{ SI}$$

$$r_{\text{whole}} = d_{\text{galaxy}}/2 \approx 6,65 \cdot 10^{20} \text{ m}$$

$$M_{\text{whole}} = 4,8 \cdot 10^{41} \text{ kg}$$

$$M_{\text{whole}} = 16 * M_{\text{core}} > \text{Brighting mass}$$

Here is **dark matter**, a challenge for researchers !!😊:::😊!!



# Yes, dark matter proposed by the astronomer Vera Rubin in the seventies

*(A pretty princess rescues a prince ; her clothes are all in a mess)*

*When the Prince saw her, he said : « You are very dirty and look like a paperbag; please, go and get cleaner before I can marry you. ».*

*The princess answered: « So don't I! » She would have been a great scientist!*



*Paper bag Princess, de Robert Munsch, traduction française *La princesse dans un sac*  
Bright galaxies, dark matter, de Vera Rubin.*